Off-Axis Reflective Optics for EO/IR Camera Onboard CubeSat:

Linear Astigmatism Free - Three Mirror System (LAF-TMS)

2024 CubeSat Developers Workshop

2024 April 23-25, CalPoly, San Luis Obispo, CA

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Inyoung Hwang, Kyung-Su Na (Agency for Defense Development, Korea)

Background

Soojong Pak (CV)

EO
(**E**lectro-**O**ptics)

IR
(**I**nfra**R**ed)

■ **Educations**

1990 Feb   B.S. Astronomy, Seoul National University, Korea

1997 Aug   PhD. Astronomy, Univ of Texas at Austin, US

■ **Job Experiences**

1997 Aug – 1998 May   Postdoc, Max-Planck-Institut für extraterrestrische Physik, Germany (Infrared Spectrograph, SINFONI)

1998 Sep – 2002 Dec   Assistant Prof., Astronomy, Seoul National University

2001 Aug – 2002 Aug   Visiting Associate Professor, ISAS/JAXA, Japan (Space Infrared Telescope, AKARI)

2002 Dec – 2006 Feb   Senior Researcher, Korea Astronomy and Space Science Institute (Space Infrared Telescope, SPICA)

2006 Mar – Now   Professor, Astronomy and Space Science, Kyung Hee University

(Astronomical Optical and Infrared Instrumentation and Observation)

Electromagnetic Wave (EO/IR Bands)

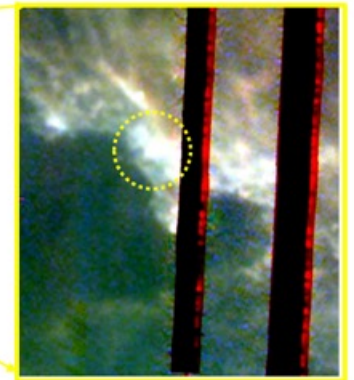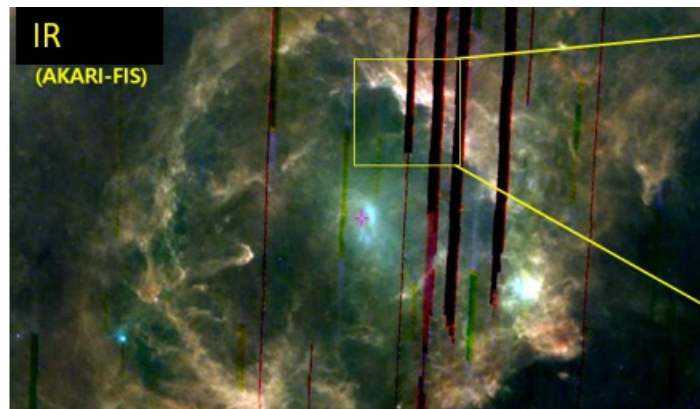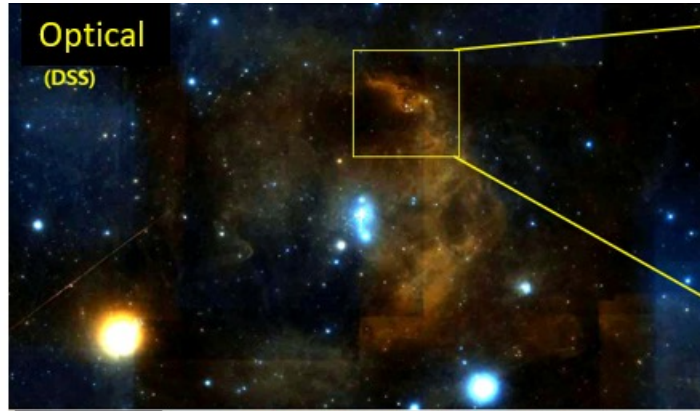| Band	Full Name	λ [μm]	Sensor	Optics
EO	Visible	0.4 – 0.7	Si	
NIR	Near-infrared	0.7 – 1.1	Si	
SWIR	Short-Wavelength Infrared	1.1 – 3	InGaAs, HgCdTe (MCT)	
MWIR	Mid-Wavelength Infrared	3 – 5	MCT, InSb (Cooled Photoconductor)	Si, Ge, ZnSe, ZnS F/D < 5
LWIR	Long-Wavelength Infrared	8 – 14	(Uncooled Microbolometer)	Chalcogenide, Ge F/D < 1.2

reflected radiation

thermal radiation

Driggers et al. (2022, Introduction to Infrared and Electro-Optical Systems) classifies that **EO** systems are those that respond to wavelengths within the 0.4 to 3-mm region, where the light collected by an EO sensor was reflected by objects in the scene. The **MWIR and LWIR** band imagers are called forward-looking infrared (FLIR) systems or imaging infrared (IIR) sensors.
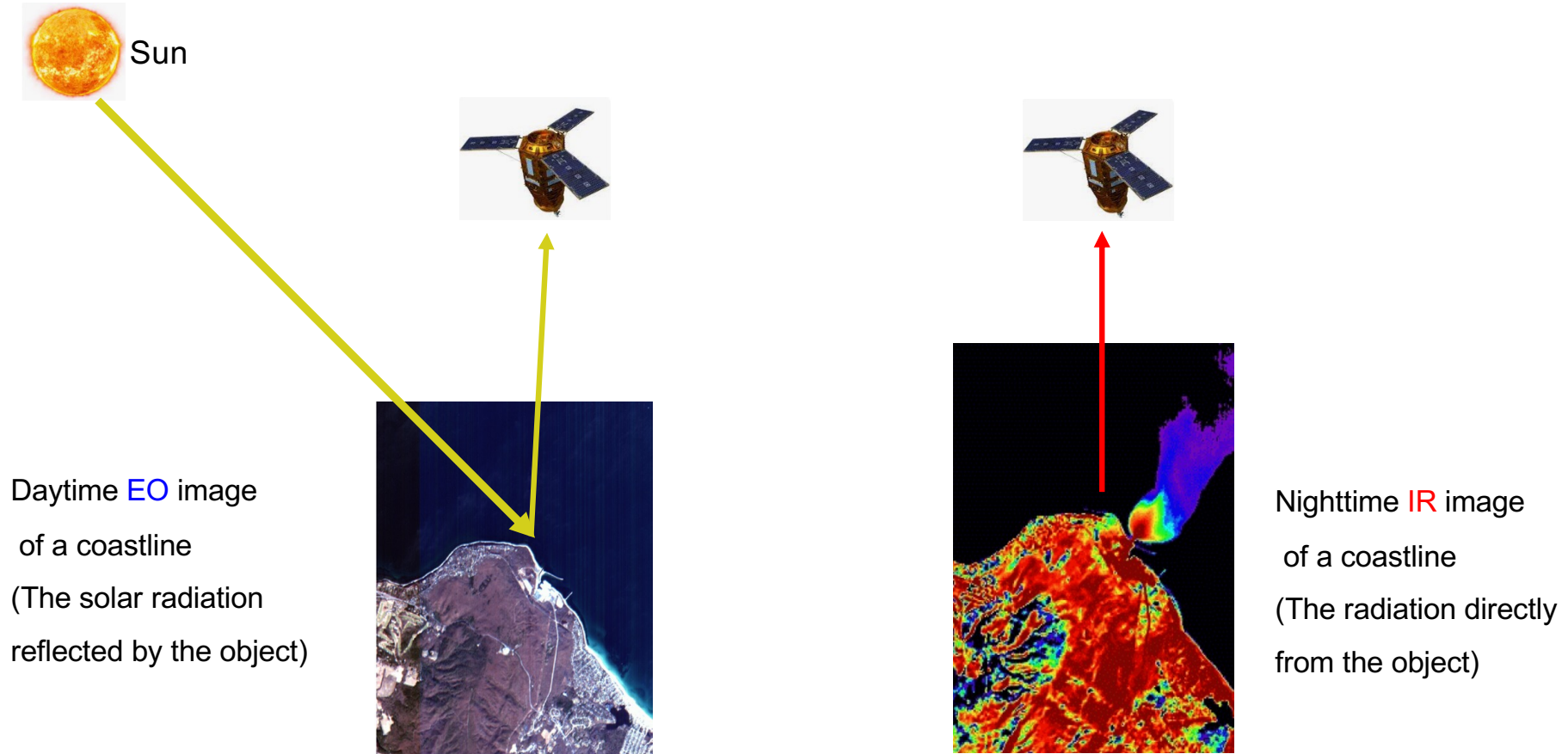
Optical & IR Astronomy

Star Forming Molecular Cloud (λ Ori)

Optical
(DSS)

IR
(AKARI-FIS)

Space-based EO/IR Remote Sensing (Surveillance Reconnaissance)

Sun

Daytime EO image
of a coastline
(The solar radiation
reflected by the object)

Nighttime IR image
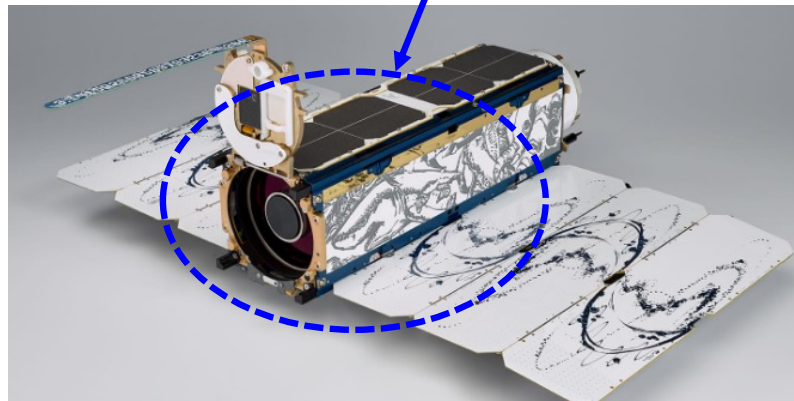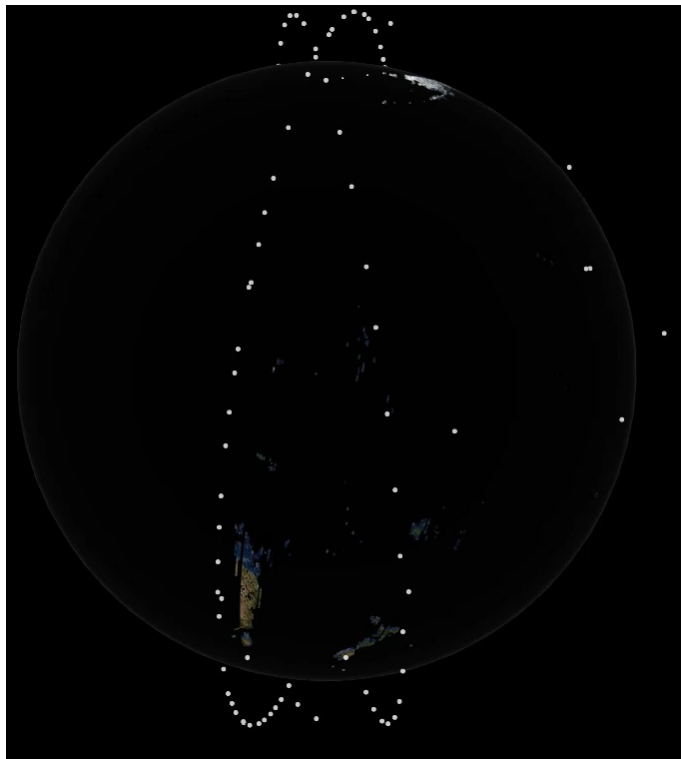of a coastline
(The radiation directly
from the object)

EO Camera on CubeSat

- Planet Labs launched 452 CubeSats (3U).

Catadioptric system (???) (ON-Axis Reflective & Refractive Corrector)

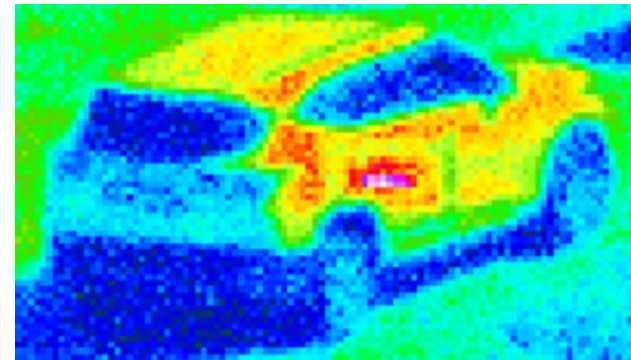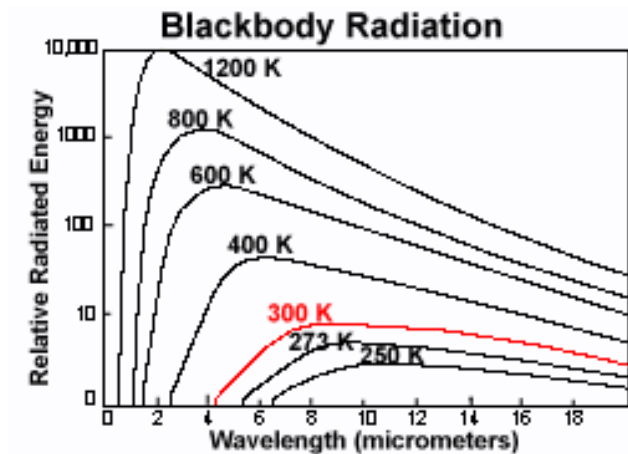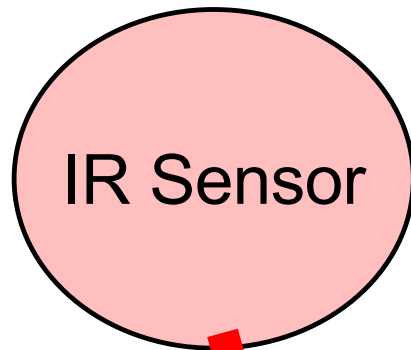# IR Technology

IR Radiation (Planck Function)

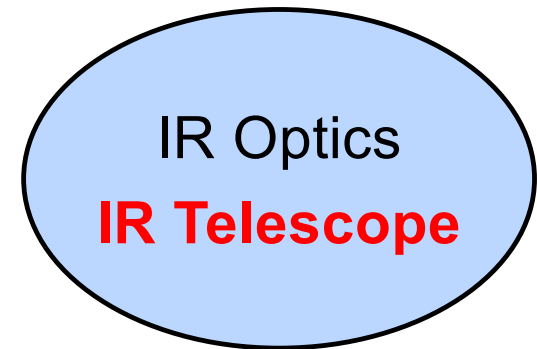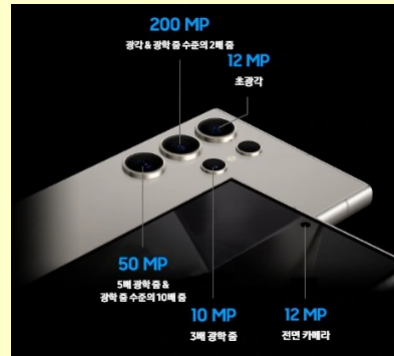$$I_\lambda(T) = \boldsymbol{\varepsilon}\, \frac{2hc^2}{\lambda^5} \frac{1}{\exp(hc/k\lambda\boldsymbol{T}) - 1}$$

*IR Radiation is a function of **emissivity (ε)** and **temperature (T)**.*

IR Camera = IR Sensor + **IR Optics**

IR Sensor

Samsung Galaxy S24 Smart Phone

IR Optics
IR Telescope

Requirements of **IR** Telescope

- Optical Resolution $\approx 1.22 \, \frac{\lambda}{D} \, h$

  Small Spatial Resolution @ D ↑ and λ ↓
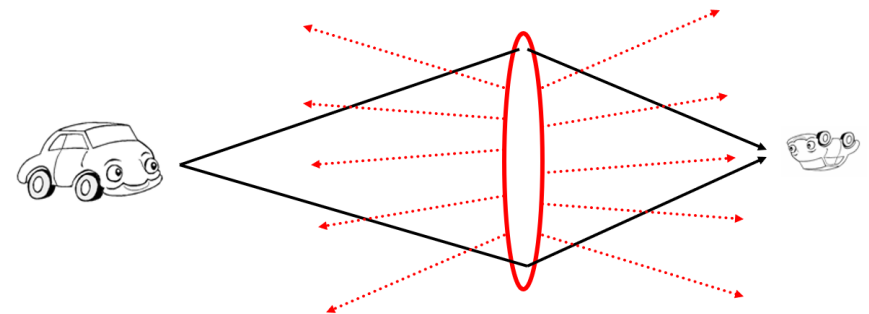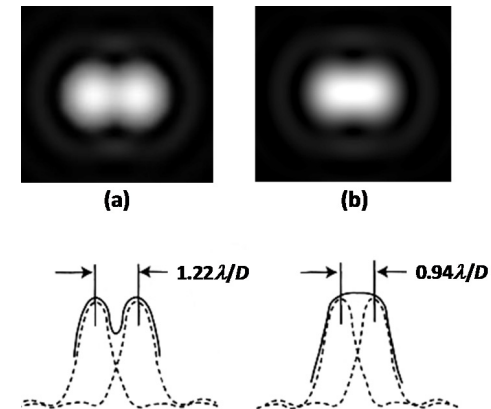
  *==> IR needs **large D** optics.*

- Radiometry

  IR emission from optics increases the noise.

  *==> IR needs **small F/D** ratio optics,*

  e.g., fast optics.
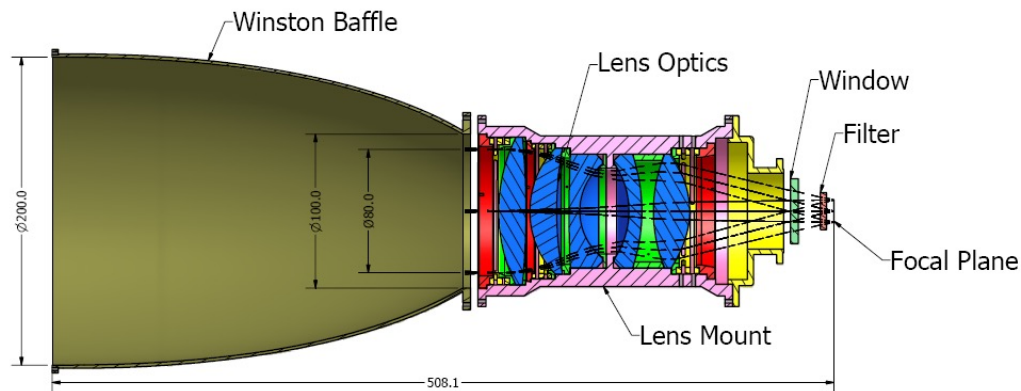

(a)　　　　　(b)

1.22λ/D　　　0.94λ/D

Refractive IR Telescope

Example of MIRIS/STSAT-3

- Developed by Korea Astronomy and Space Science Institute

- Lunched in 2013 Nov

- Astronomical Survey at 1.1 – 1.6 um.

miris.kasi.re.kr/miris/pages/instrument/

MIRIS   News   Instrument   Surveys   Data   Galle

Instrument

Summary

The following table summarizes the specification of MIRIS.

| Item	Parameter	Specification	Remark
Telescope	Aperture	80 mm	
	F-number	F/2	
	Focal length	160 mm	
	Field of View	3.67°×3.67°	
Detector	Teledyne PICNIC (HgCdTe)		
	Detector array	256 × 256	
	Pixel size	40 μm	
	Pixel scale	51.6"	
Filters	Broadband	1.1 & 1.6 μm	$\Delta\lambda/\lambda \gtrsim 0.5$
	Narrowband	PAAL & PAAC	
Orbit	Low Earth, Sun-synchronous orbit		
	Altitude	about 620 km	
	Inclination	97.8°	
	MLTAN [1]	22.3 o'clock	

[1] Mean local time of ascending node

Refractive IR Telescope

Pros

- Good *optical Performances*
- Confirmed *fabrication methods* for lens
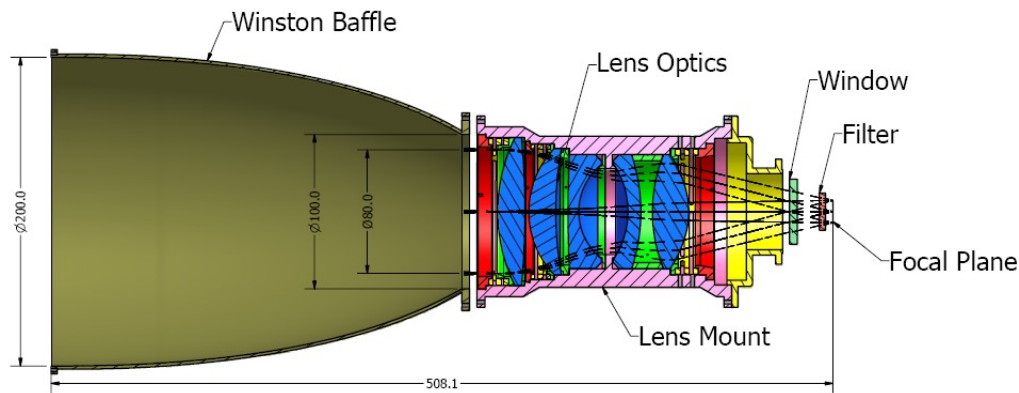
Cons

- Limited *lens materials @ > 5* μm
- Heavy weight
- Complex *opto-mechanical* structures

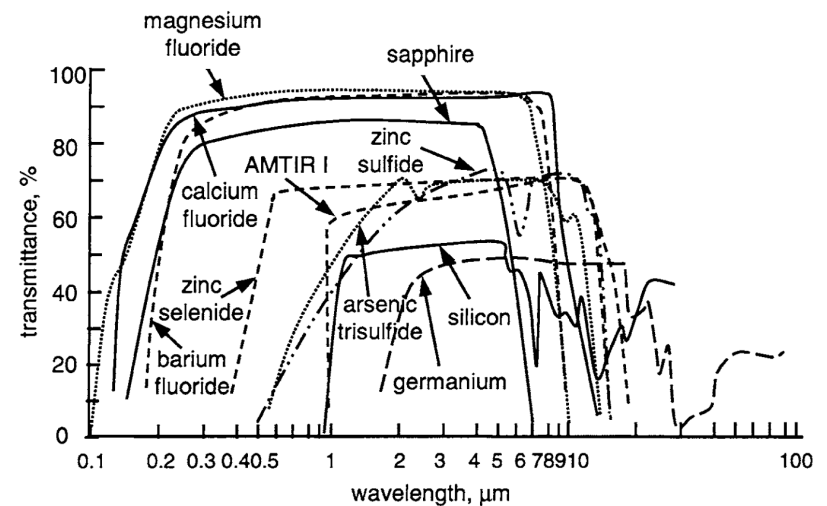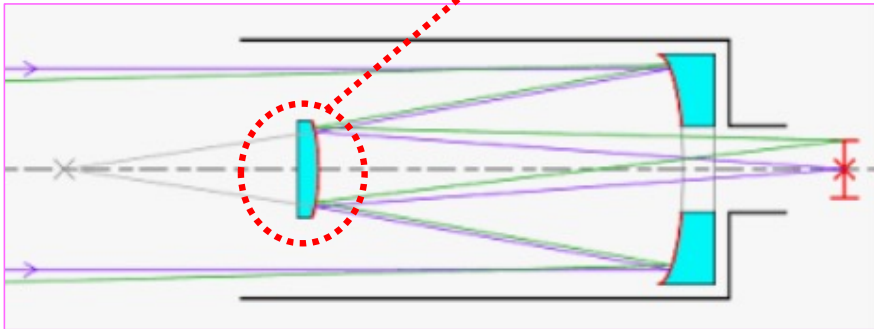Figure 12.13 in Robert E. Fisher et al. (2008, Optical System Design)

On-Axis Reflective Telescope

Cons

- ***Central Obstruction*** by secondary mirrors
  - ✓ Limited FoV: Smaller F/D ratio needs larger secondary mirrors.
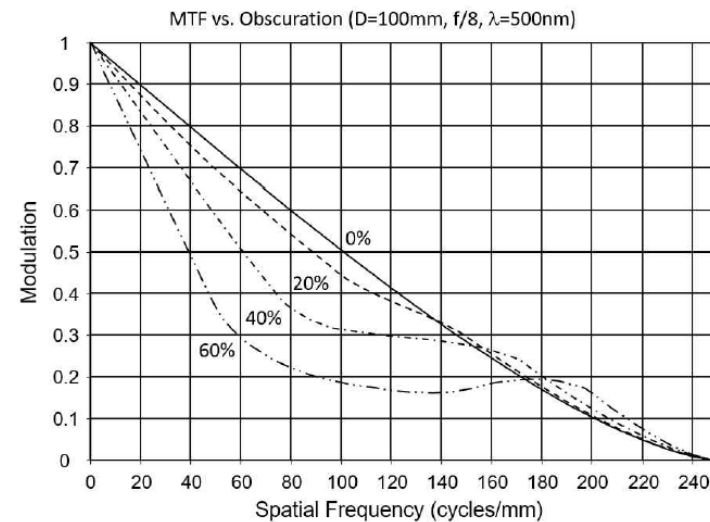 - ✓ Diffraction by the secondary mirror degrades the optical resolution (MTF).

Pros

- Confirmed ***fabrication methods*** for mirrors.
- Easy optics ***alignment***

Fig. 4 in Pak, Chang, and Lee (2023, Journal of Korean Space Association for National Defense)
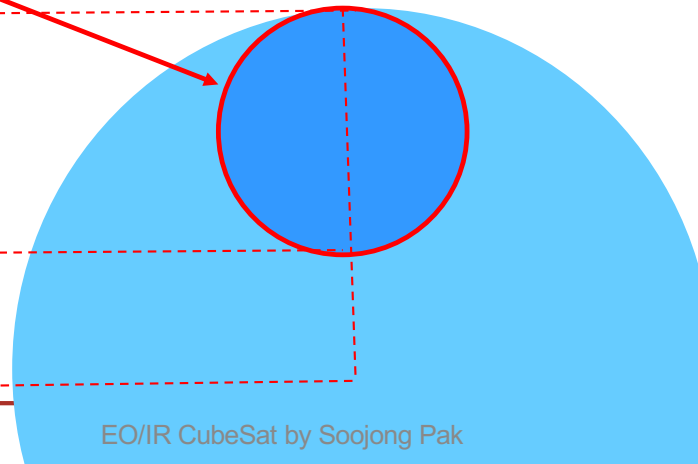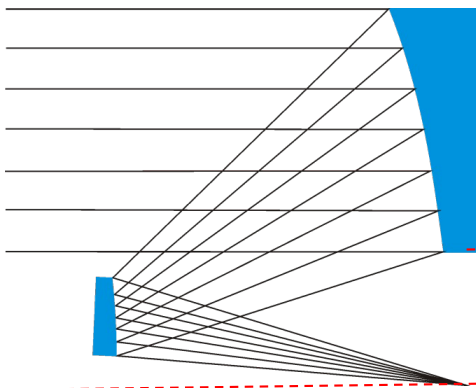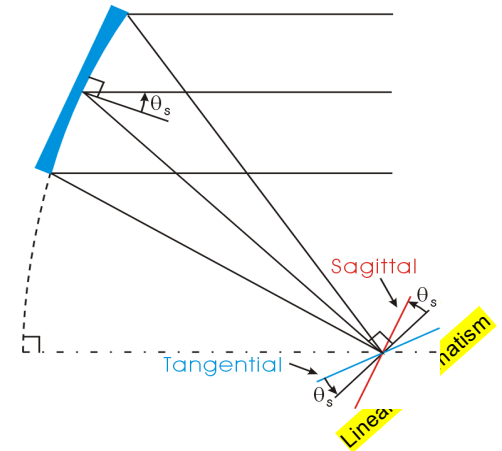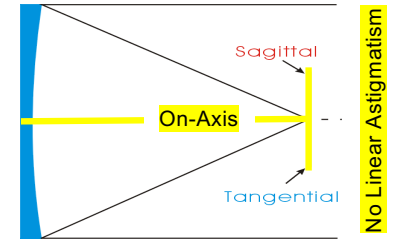
OFF-Axis Reflective Telescope

Pros

- **NO abstraction** of secondary mirror
- Confirmed **fabrication methods** for mirrors

Cons

- High **linear astigmatism**

Innovative Off-Axis Reflective Telescope

with *Linear Astigmatism Free (LAF)* Condition

Innovative Off-Axis Reflective Design (*a.k.a. Chang Theory*)

- Dr. Seunghyuk Chang found analytic solutions with which the linear astigmatism is eliminated, using ***the optical path length method*** by Karl Schwarzschild in 1905.
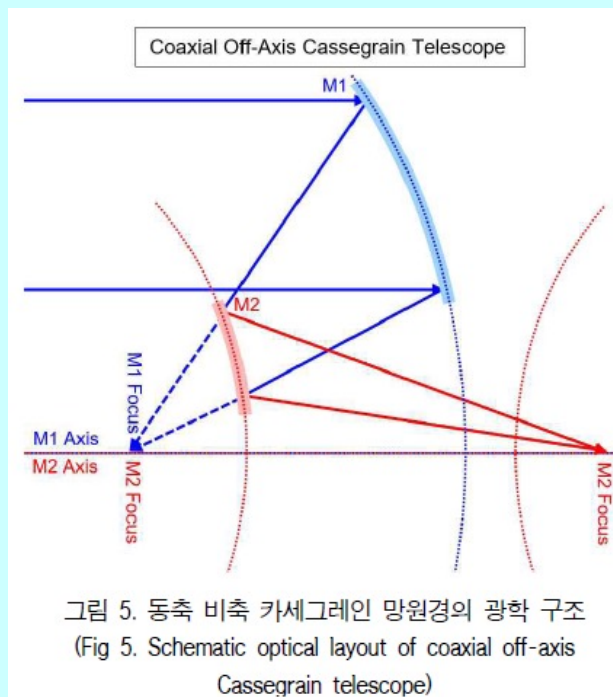

- References

  - **S. Chang 2003, PhD Thesis, University of Southern California**
    "Geometrical theory of aberrations for Classical Offset Reflector Antennas and Telescopes"

  - S. Chang and A. Prata, Jr. 2005, Journal of the Optical Society of America A 22, 2454-2464
    "Geometrical theory of aberrations near the axis in classical off-axis reflecting telescopes"

  - S. Chang, J. H. Lee, S. P. Kim, H. Kim, W. J. Kim, I. Song, and Y. Park, 2006, Applied Optics 45, 484-488
    "Linear astigmatism of confocal off-axis reflective imaging systems and its elimination"

  - S. Chang, 2015, J. Opt. Soc. Am. A 32, 852-859
    "Linear astigmatism of confocal off-axis reflective imaging systems with N-conic mirrors and its elimination"
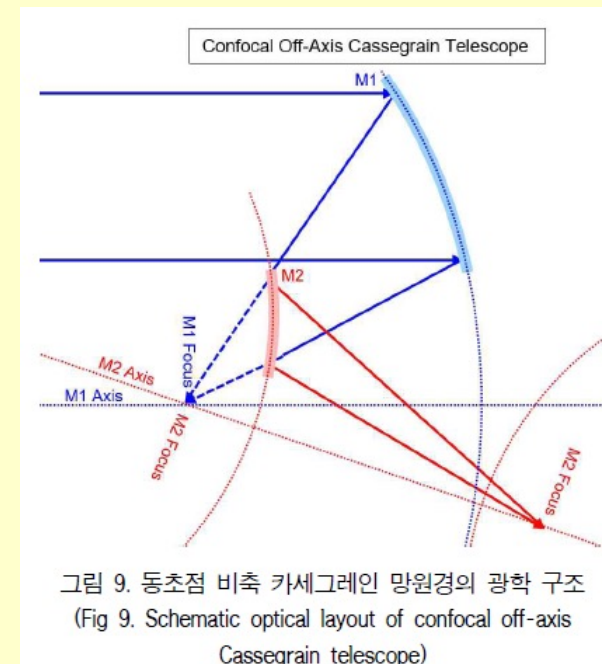
Coaxial Off-Axis vs. **Confocal** Off-Axis (Chang Theory)

Previous Theory: Coaxial Off-Axis

그림 5. 동축 비축 카세그레인 망원경의 광학 구조
(Fig 5. Schematic optical layout of coaxial off-axis Cassegrain telescope)

Chang's Theory: Confocal Off-Axis

그림 9. 동초점 비축 카세그레인 망원경의 광학 구조
(Fig 9. Schematic optical layout of confocal off-axis Cassegrain telescope)

Vertex Equation in Geometrical Optics

- **Vertex equation in the Localized coordinate system** at (x_0', z_0')
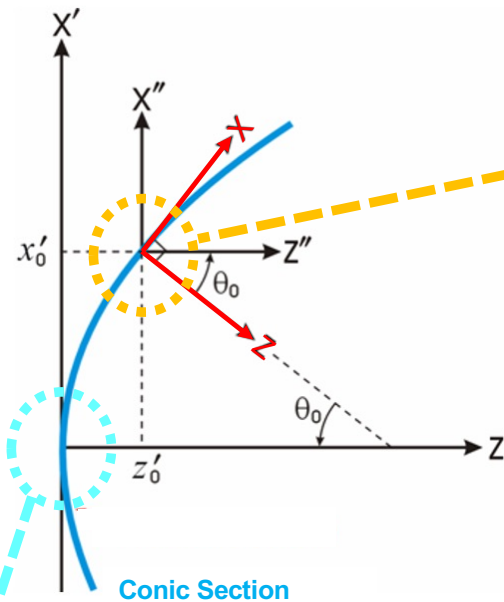
$$(1 - K\cos^2\theta_0)z^2 -$$

$$\left(xK\sin 2\theta_0 + \frac{2R}{\sqrt{1 - K\sin^2\theta_0}} \right) z +$$

$$(1 - K\sin^2\theta_0)x^2 + y^2 = 0$$

Conic Section

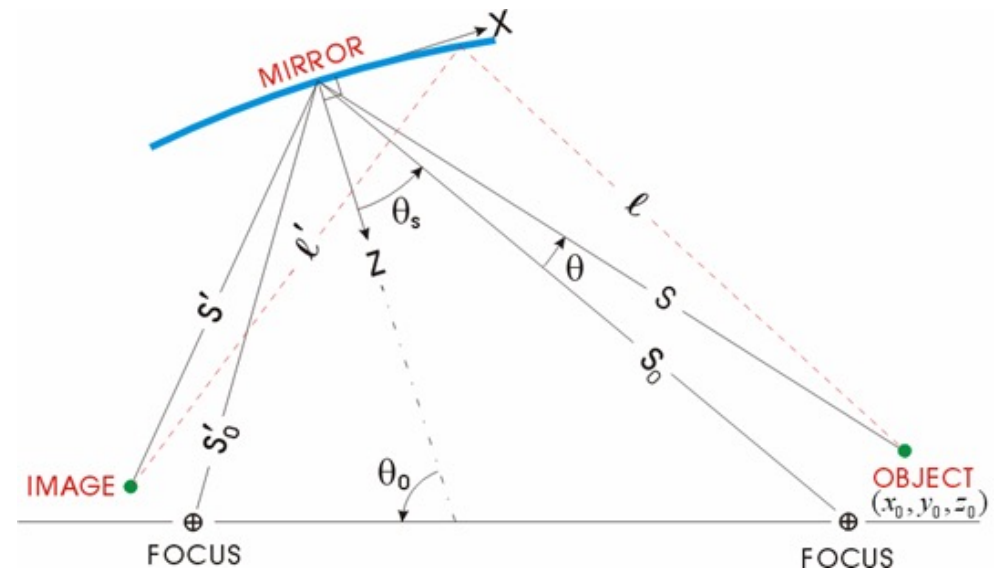- Vertex equation of conic sections of revolution :

$$\rho'^2 - 2Rz' + (1 - K)z'^2 = 0$$

Optical Path Length (OPL)

- The OPL is constant in a perfect focusing mirror.

- The variance of the OPL yields aberrations

$$OPL = \ell + \ell' = s + s' + A_1 x^2 + A_1' y^2 + A_2 x^3 + A_2' xy^2 + O(4)$$

$$\underbrace{}_{\text{Astigmatism}} \quad \underbrace{}_{\text{Coma}}$$

Astigmatism   Coma

Aberrations of Two-Mirror Off-Axis Telescope

Coma $ATC = \theta \dfrac{3x_0^2}{4f^2}$ The 3rd order Coma is identical to the On-Axis telescope.
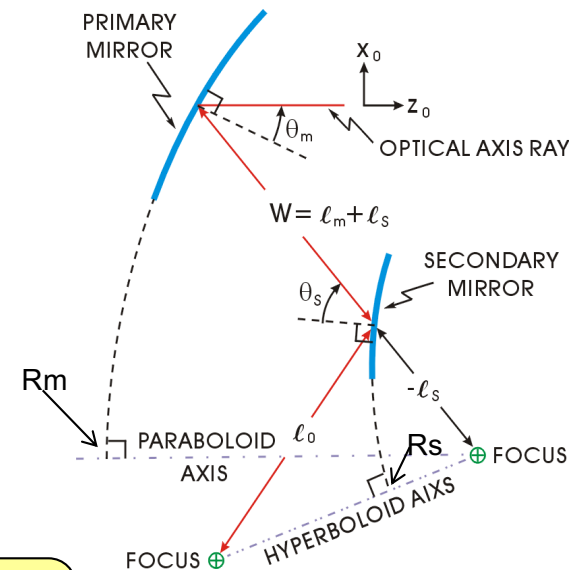
Astigmatism

$$\frac{\Delta s'}{f} = 2\theta \left(\frac{\ell_m}{\ell_s} \frac{\sin 2\theta_m}{R_m} - \frac{\sin 2\theta_s}{R_s} \right) \ell_0 - \frac{\theta^2}{\ell_0} \left[W - f \left(1 + \tan\theta_m \tan\theta_s \right) \right]$$

3rd Order Astigmatism

Linear Astigmatism

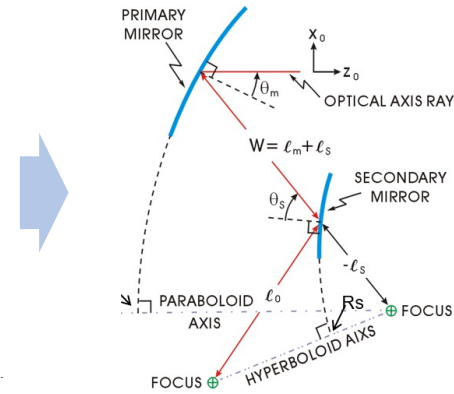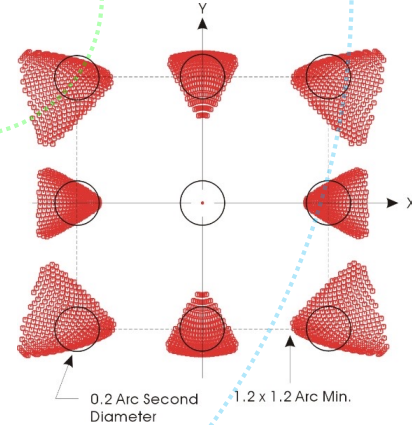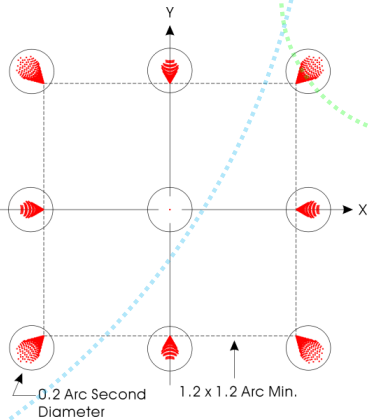Linear Astigmatism is eliminated at $\quad \dfrac{\ell_m}{R_m} \sin 2\theta_m = \dfrac{\ell_s}{R_s} \sin 2\theta_s$

PRIMARY MIRROR

x_0

z_0

θ_m

OPTICAL AXIS RAY

$W = \ell_m + \ell_s$

SECONDARY MIRROR

θ_s

Rm

$-\ell_s$

PARABOLOID AXIS

ℓ_0

Rs

FOCUS

HYPERBOLOID AIXS

FOCUS

Example: F/8 Classical Cassegrain

축대칭
On-Axis

동축 비축
Coaxial Off-Axis
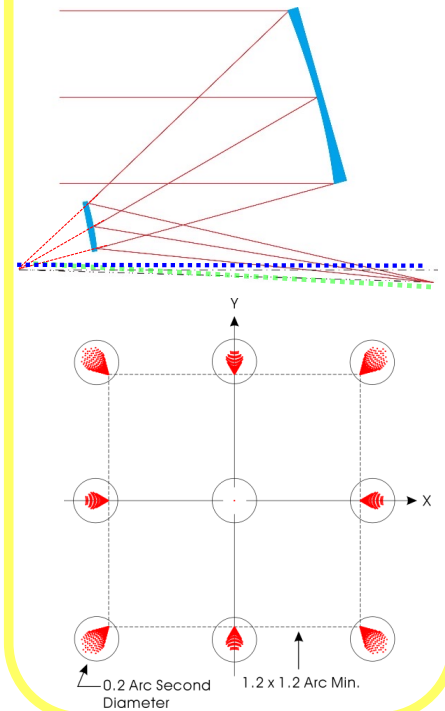
동초점 비축
Confocal Off-Axis)

$$\frac{\Delta s'}{f} = 2\theta \left(\frac{\ell_m}{\ell_s} \frac{\sin 2\theta_m}{R_m} - \frac{\sin 2\theta_s}{R_s} \right) \ell_0 - \frac{\theta^2}{\ell_0} \left[W - f \left(1 + \tan\theta_m \tan\theta_s \right) \right]$$

Linear Astigmatism

3rd Order Astigmatism

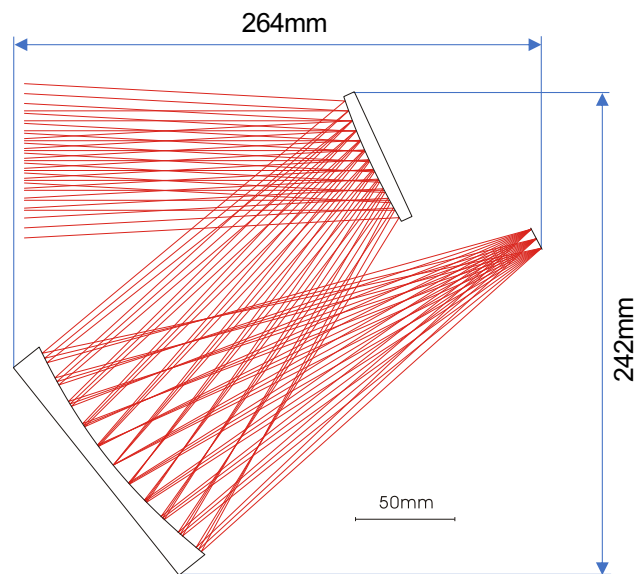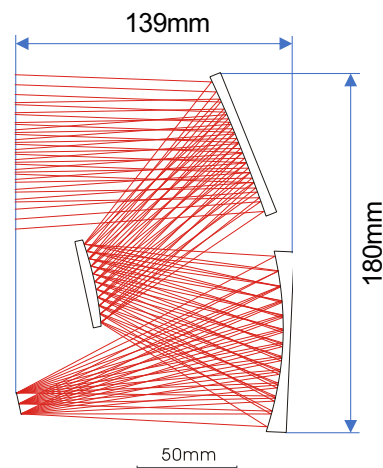$\frac{\ell_m}{R_m} \sin 2\theta_m = \frac{\ell_s}{R_s} \sin 2\theta_s$ 의 조건에서 선형비점수차가 제거된다.

LAF 2-Mirror vs. 3-Mirror System

D50mm F/2 Wide Field Space Telescope
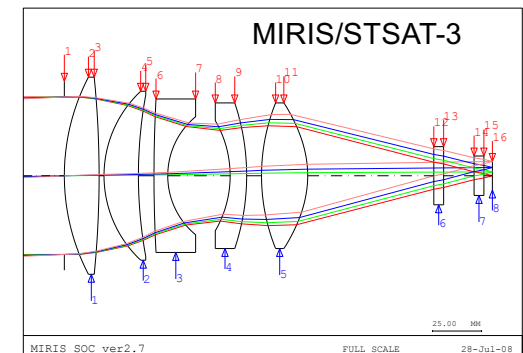

Linear Astigmatism Free 2-Mirror Design
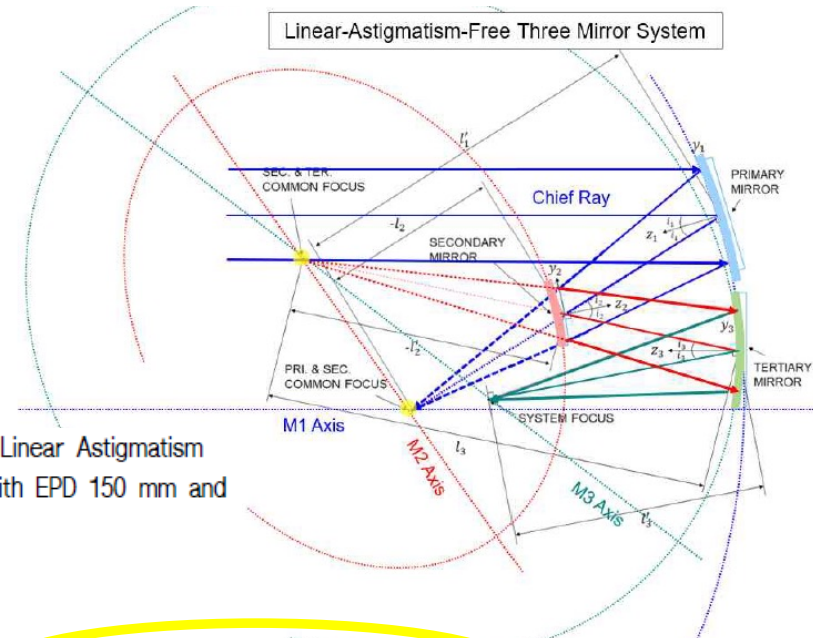(Schwarzschild-Chang Type)

Kim, Pak, Chang et al., 2010

LAF-TMS:
Linear Astigmatism Free
Three Mirror System

MIRIS/STSAT-3

Three Mirror Anastigmat (TMA) vs LAF-TMS

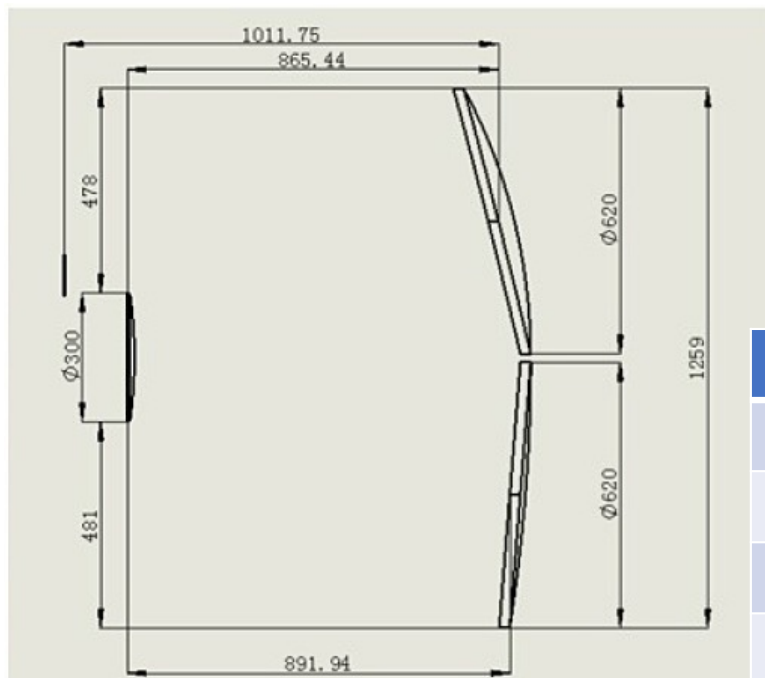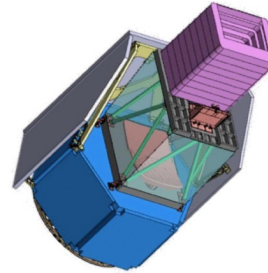Linear-Astigmatism-Free Three Mirror System

(Fig 15. Schematic optical layout of Linear Astigmatism Free-Three Mirror System LAF-TMS with EPD 150 mm and f-number 3.3)

|	TMA (Coaxial Off-Axis)	LAF-TMS (Confocal Off-Axis)
Design Process	(1) Start from Paul-Becker type (On-axis) (2) Select the off-axis part from the PB (3) Optimize the mirror, etc. numerically Focused on **third-order aberrations** (Spherical, Coma, Third-order astigmatism)	(1) Find Linear Astigmatism Free Condition (2) Optimize the mirrors numerically Focused on **other third-order aberrations**
Linear Astigmatism	Can be reduced by optimization (**Not zero**)	**Elliminated**

Example: LAF-TMS vs. TMA (Messier, D400mm F/2)

TMA (Three Mirror Anastigmat)
Coaxial Off-Axis

LAF-TMS
Linear Astigmatism Free
Three Mirror System
Confocal Off-Axis

	TMA	LAF	LAF/TMA
M1	620	491	0.79
M2	300	223	0.74
M3	620	461	0.74
mass ratio			0.4
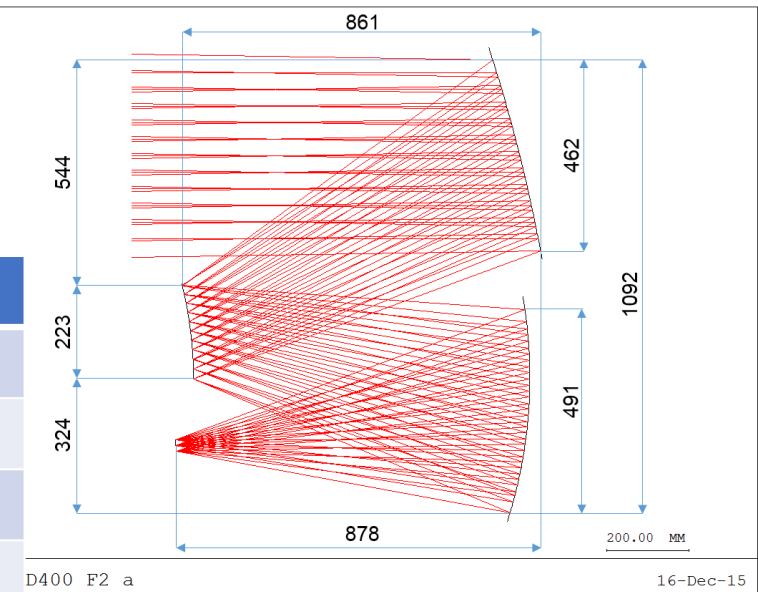
* Hugot, Wang, Valls-Gabaud et al., 2014, SPIE 9143, 9143X (https://doi.org/10.1117/12.2057461)
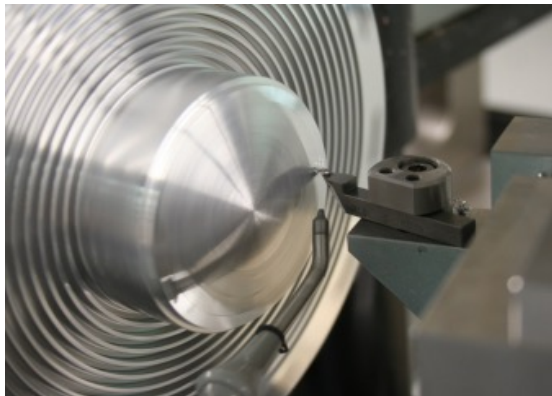
Applications of
Linear Astigmatism Free (LAF) Space Telescopes

(1) Fabrication of Aluminum Freeform Mirror

- XY Polynomial Mirrors: Quadratic surface composed of polynomials expanded into monomials of $x^m y^n$ with degree m, n ($m + n \leq 10$), where C_j is the monomial coefficient. $z = \sum_{j=2}^{66} C_j \, x^m y^n$, where $j = \frac{(m+n)^2 + m + 3n}{2} + 1$

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[5]Material Machining Team, Medical Device Development Center, Cheongwon 363-951, South Korea
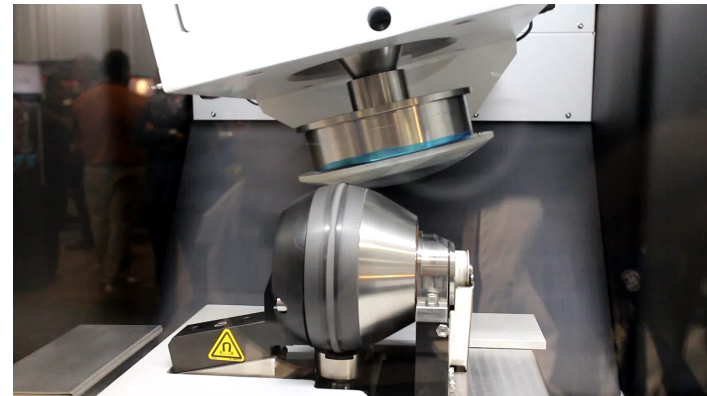[6]Yoonseul Inc., 80 Daehwa-ro 32-beon-gil, Daedeog-gu, Daejeon 34364, South Korea
[7]College of Engineering, Kyung Hee University, Yongin 446-701, South Korea
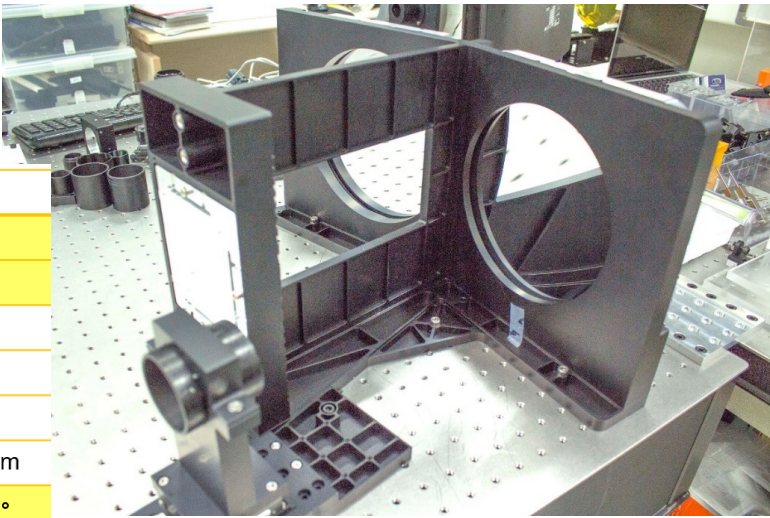*Corresponding author: chang@offaxis.co.kr

Single Point Diamond Turning

Magneto Rheological Finishing

(2) Protomodel for Space IR Telescope

Parameter	Value
EPD	150 mm
EFL	500 mm
Pixel size	6 um
Pixel FOV	2.5 ″
Array Format	8K x 6K
Array Size	49 x 37 mm
FOV	5.5° x 4.1°
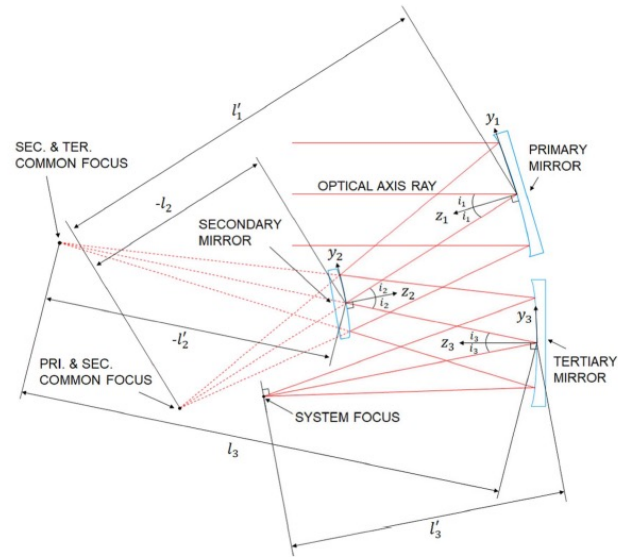
Figure 1. The optical layout of LAF-TMS. Optical path is drawn in red solid lines.
(A color version of this figure is available in the online journal.)

Development of Linear Astigmatism Free—Three Mirror System (LAF-TMS)

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[5] Omnisys Instruments AB, Västra Frölunda, SE-421 32, Sweden
[6] Korea Basic Science Institute, 169-148, Daejeon 34133, Republic of Korea
[7] Green Optics, Cheongju 28126, Republic of Korea
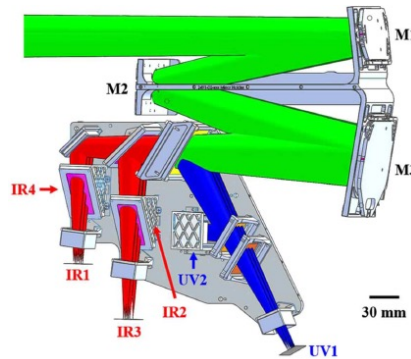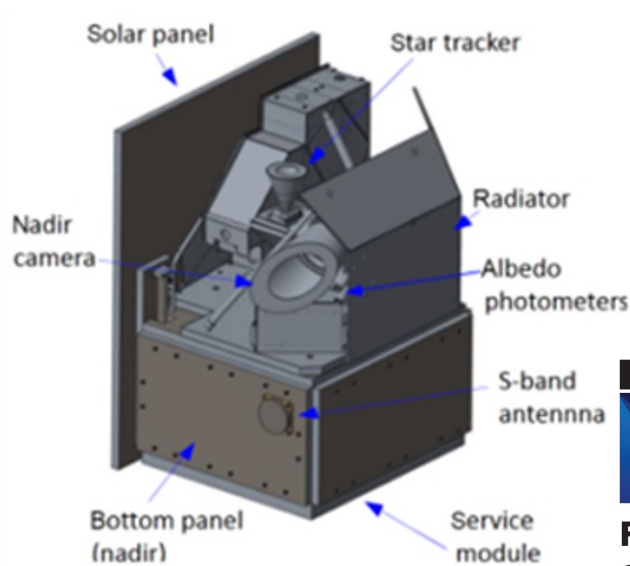[8] James C. Wyant College of Optical Sciences, University of Arizona, Tucson, AZ 85721, USA
Received 2019 November 14; accepted 2020 February 11; published 2020 March 13

(3) Swedish Science Satellite MATS

(Mesospheric Airglow/Aerosol Tomography and Spectroscopy)

- Lunched on Nov 4, 2022.

Research Article — Vol. 59, No. 17 / 10 June 2020 / Applied Optics — 5335

applied optics

Flight model characterization of the wide-field off-axis telescope for the MATS satellite

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Rocket Lab launches the Swedish MATS satellite from New Zealand aboard an Electron rocket

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.ab USA Inc. has successfully launched its 32nd Electron mission to he firm's 152nd satellite to orbit, a science payload for the *Swedish ! Space Agency*. The MATS satellite was deployed to its 585 km. circular Electron following lift-off at 17:27 UTC.

(4) IR Spectroscopic Imaging System for UAV

- IR Telescope Optics for MWIR/LWIR dual sensor hyperspectral Camera onboard unmanned aerial vehicle (UAV).

- Material: Aluminum 6061-T6

- Weight 3 kg

- Part of Unmanned Vehicle Core Technology Development Project funded by National Research Foundation of Korea.
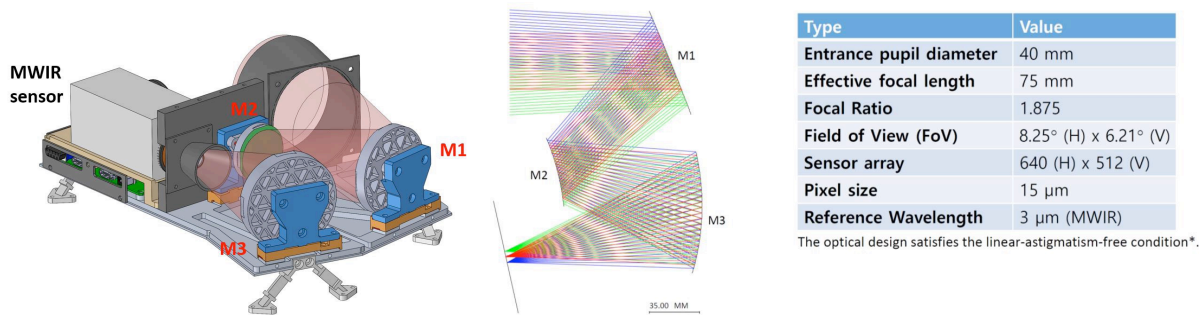
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Wide-wide linear astigmatism free-three mirror system (LAF-TMS) enabling wide field-of-view and spectral bandwidth detection

Changgon Kim, Dohoon Kim, Jimin Han, Seunghyuk Chang, Woojin Park, et al.

Type	Value
Entrance pupil diameter	40 mm
Effective focal length	75 mm
Focal Ratio	1.875
Field of View (FoV)	8.25° (H) x 6.21° (V)
Sensor array	640 (H) x 512 (V)
Pixel size	15 μm
Reference Wavelength	3 μm (MWIR)

The optical design satisfies the linear-astigmatism-free condition*.

Summary

- We are leveraging astronomical infrared techniques to space IR telescopes for both astronomy and remote sensing applications.

- The optical technology for space-based IR telescopes is crucial.

- We developed noble technologies including:

  - Optical design for Linear Astigmatism Free off-axis reflective telescopes

  - Opto-mechanical design for space-based telescopes

  - Fabrication of aluminum freeform mirrors for off-axis telescopes

  - Alignment of freeform mirrors in off-axis telescopes

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Thank You