

# 10th Annual Cubesat Developer's Workshop

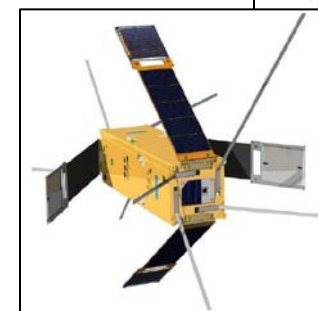
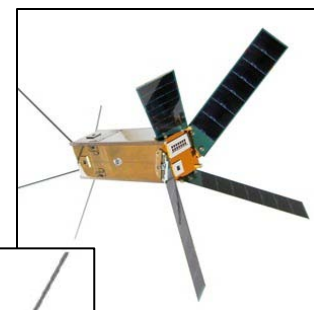
## Design optimization of a Solar Panel Angle and its Application to CubeSat 'CADRE'

**Dae Young Lee, James W. Cutler**

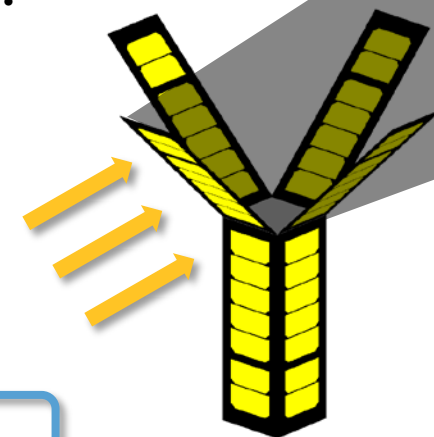
# Introduction

- **Many CubeSats are power constrained.**
  - There is not enough space for the solar cell installation.
  - Low Earth Orbits have varying eclipse times.
  
- **Existing solutions**
  - Deployable panels : ex. ‘Space-dart’ configuration
  
- **Question : How can we maximize the utility of deployable panels?**
  - What is the best pointing angle for the panels?
    - Anigstein et al[1]. developed a optimal pointing angle decision methodology.
    - But they assumed no shadow on panels.
  - How do you assess the impact of solar panel shadow?
    - Consideration of the shadow effect is important during the satellite design.
    - More deployable panel can cast more shadows.

Delfi-NEXT



Delfi-C3



CADRE

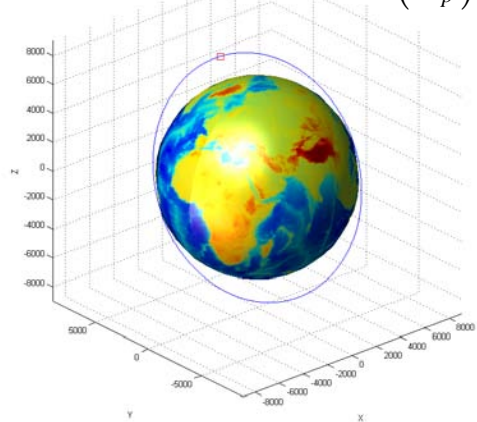
• **Goal : To develop a process that determines static solar panel angles for optimal power generation**

[1]”Analysis of Solar Panel Orientation in Low Altitude Satellites” IEEE Transactions on Aerospace and Electronic Systems VOL. 34, NO. 2 APRIL 1998

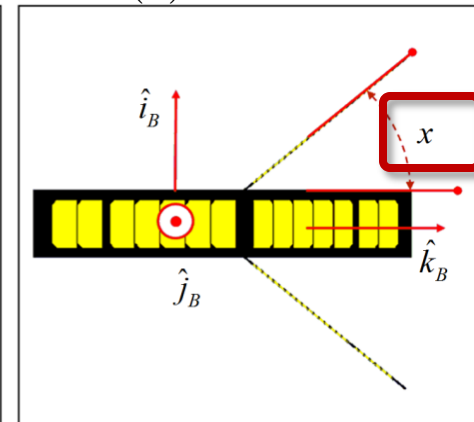
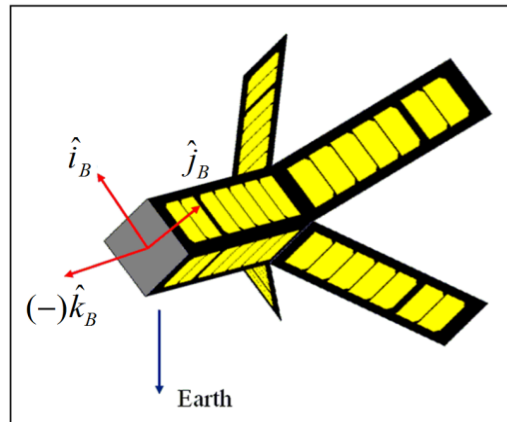
# Objective Function Candidates

- **Problem : What is the best panel angle in the given orbit parameter**

Orbit Parameter ( $O_p$ )



Design variable ( $x$ )



- **There are multiple objective functions for the power generation optimization**

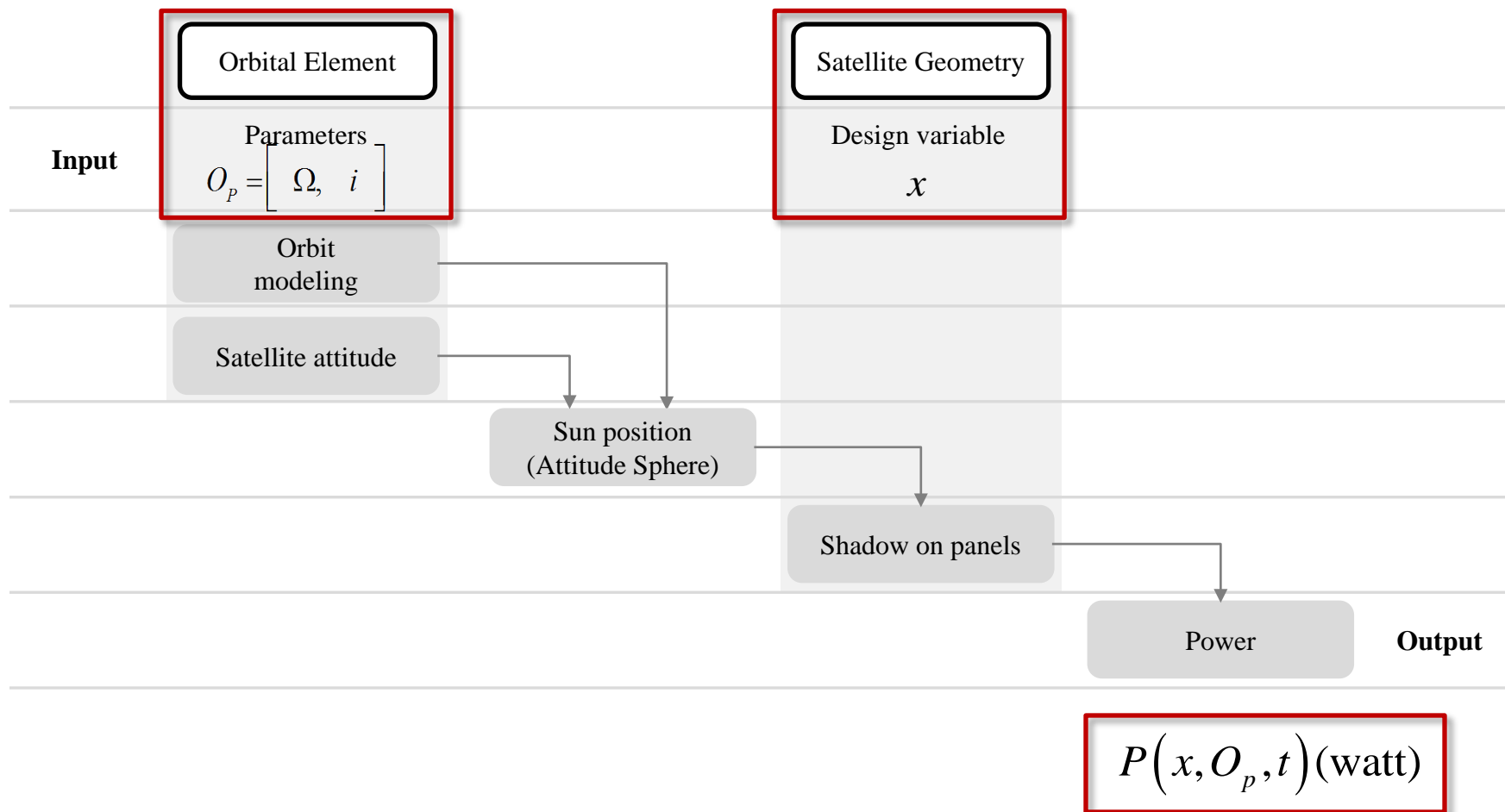
$$\max \left\{ \int_0^T P(x, O_p, t) dt, T = 1 \text{ year} \right\} - \text{Maximization of the total power generated during 1 year period}$$

$$\max \left\{ \min \left\{ \frac{1}{T} \int_{(n-1)T}^{nT} P(x, O_p, t) dt, T = 1 \text{ orbit}, n \in \left[ 0, \frac{1 \text{ year}}{T} \right] \right\} \right\} - \text{Maximization of the minimum orbit average power which was recorded during 1 year simulation period}$$

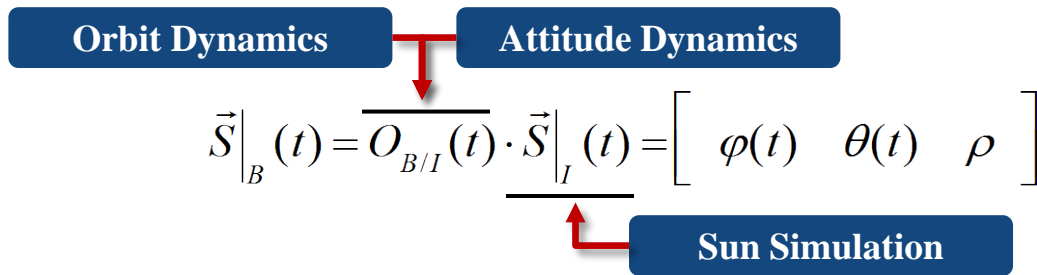
$$\max \left\{ \min \left\{ P(x, O_p, t), t \in [0, T_{orbit}] \right\} \right\} - \text{Maximization of the low limit power generated during 1 orbit period (Sun synchronous Orbit)}$$

# Simulation Process

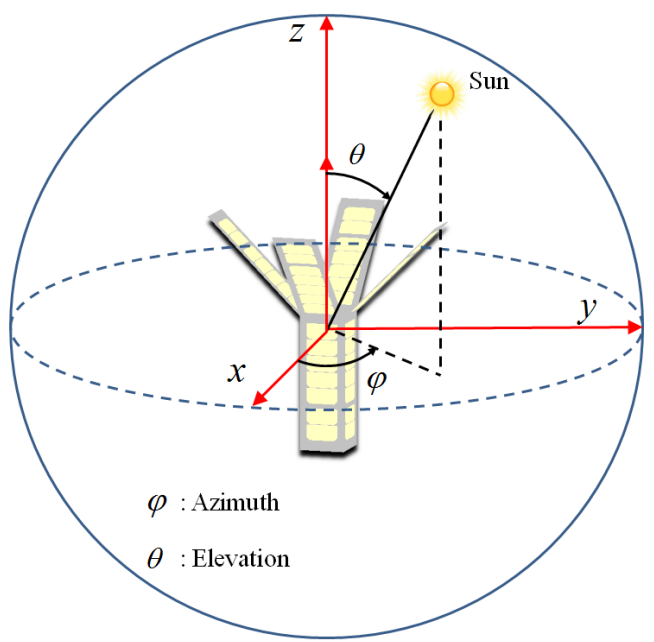
- Simulation Process for the power evaluation



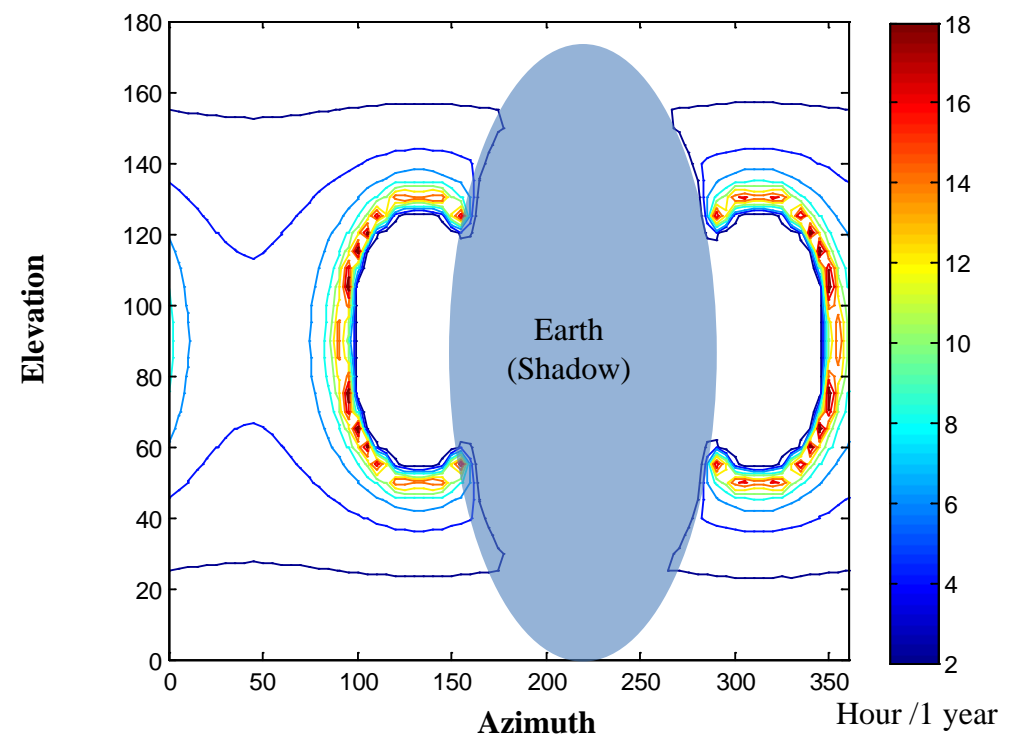
- Sun position mapping in the attitude sphere<sup>[2]</sup> can be done based on the simulation



Ex) Inc = 60°, RAAN = 90°  
03/20/2015 ~ 03/19/2016



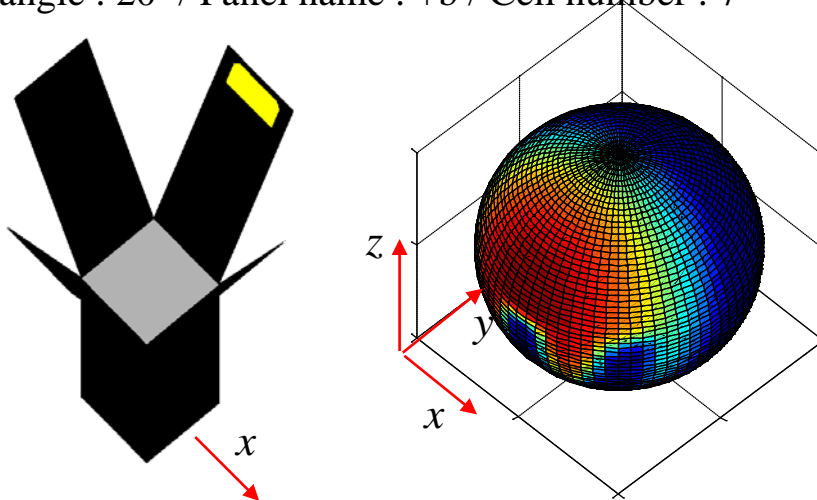
Attitude Sphere<sup>[2]</sup>



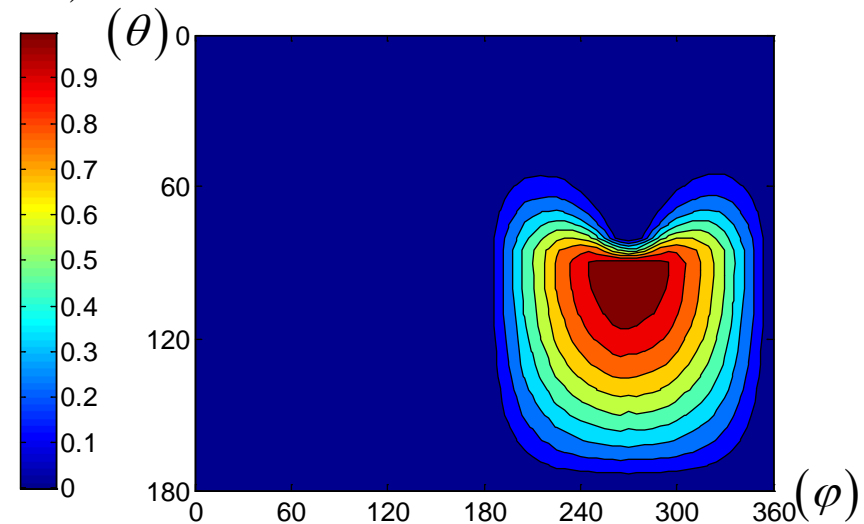
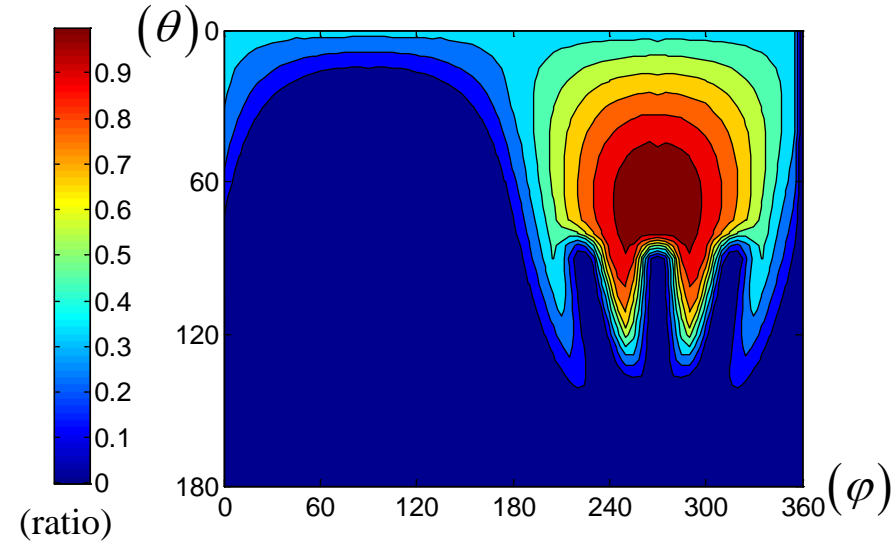
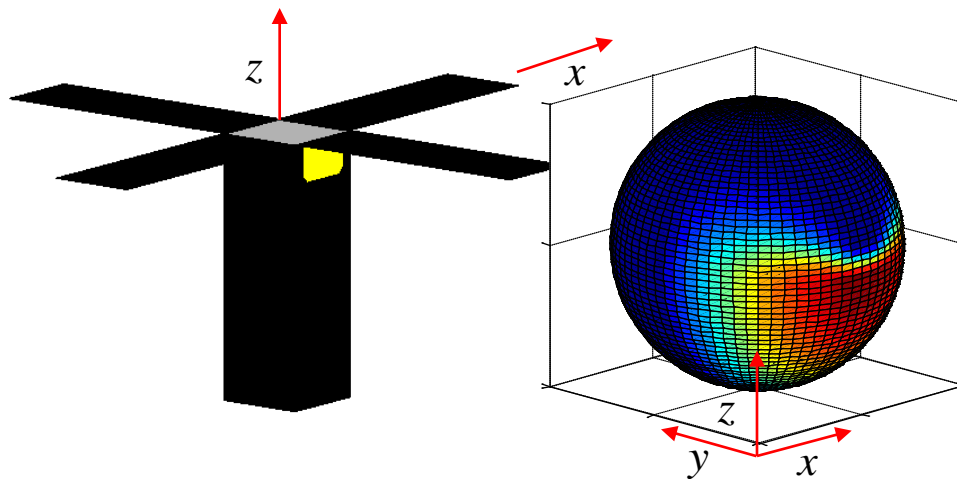
[2] J.C. Springmann and J.W. Cutler “[Optimization of Directional Sensor Orientation with Application to Photodiodes for Spacecraft Attitude Determination](#)”, Proceedings of the 23rd AAS/AIAA Spaceflight Mechanics Meeting, Kauai, Hawaii, February 2013.

- We calculate the solar cell surface area projected in the direction of the Sun
  - Using OpenGL, we calculate the area quickly and make a database .

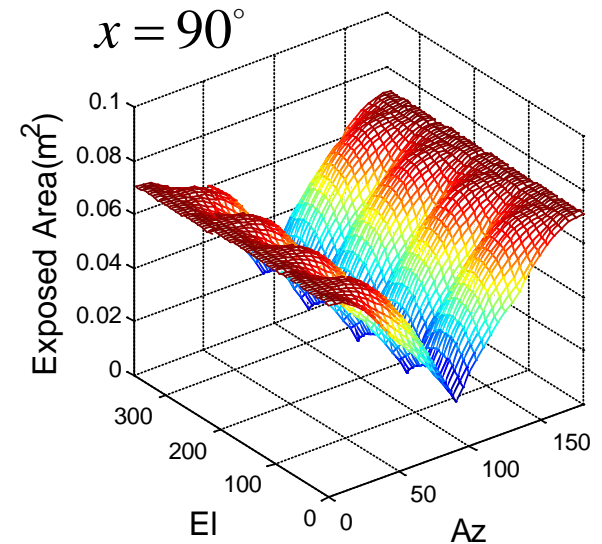
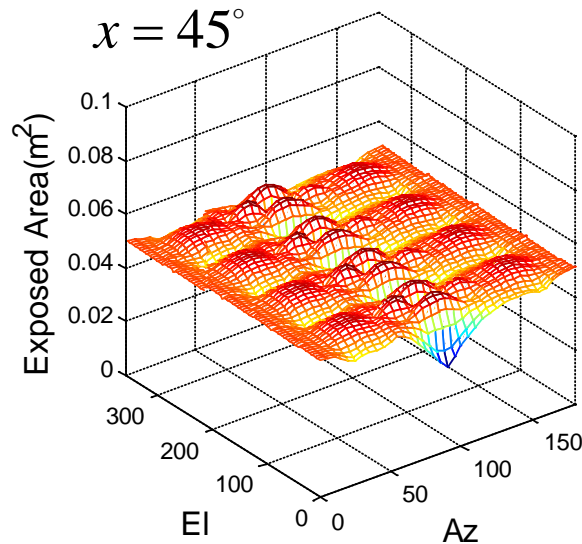
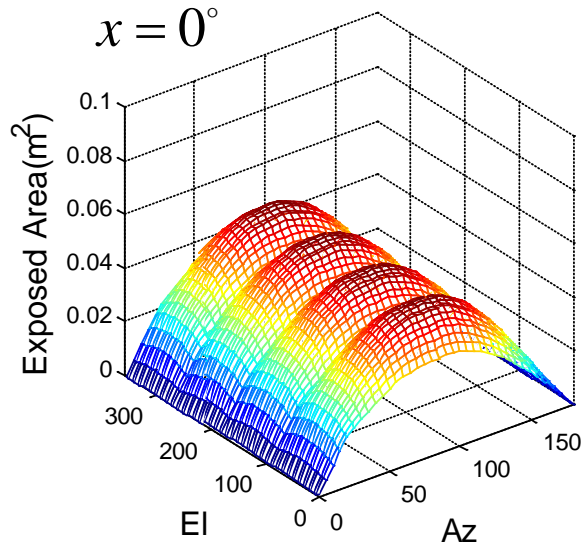
Panel angle : 20° / Panel name : +b / Cell number : 7



Panel angle : 90° / Panel name : -y / Cell number : 1



- **Sum of each cell's projected area in the attitude sphere**



- **We use a following equation to calculate the generated power by solar cells**

$$P(x, O_p, t) = S_0 \cdot \varepsilon \cdot \sum_{i=1}^{12} \sum_{j=1}^7 A_{i,j} \left( x, \varphi_{sun}(O_p, t), \theta_{sun}(O_p, t) \right)$$

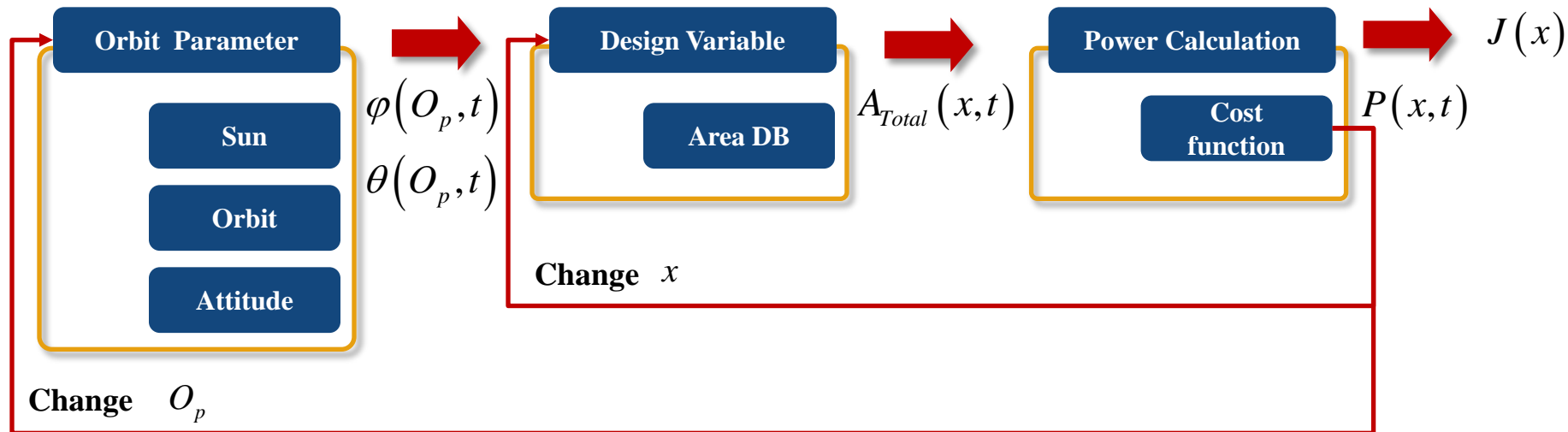
$$= S_0 \cdot \varepsilon \cdot A_{Total} \left( x, \varphi_{sun}(O_p, t), \theta_{sun}(O_p, t) \right)$$

$$S_0 \square 1366 \text{ W/m}^2, \quad \varepsilon \square 28\% \quad 0^\circ \leq x \leq 90^\circ, \quad 0^\circ \leq \varphi_{sun}(O_p, t) < 360^\circ, \quad 0^\circ \leq \theta_{sun}(O_p, t) \leq 180^\circ$$

- **It is assumed that solar power generation is proportional to the solar cell surface area projected in the direction of the Sun.**



- Panel angle value can be found out by exhaustive search on design space



- In this exhaustive searching process, the range of the panel angle  $x$  is  $0^\circ, 3^\circ, 6^\circ, \dots, 90^\circ$
- the major parameters which affect solar power generation are the inclination( $i$ ) and RAAN( $\Omega$ )
  - Because, the Sun incident angle to orbital plane is decided by the inclination( $i$ ) and RAAN( $\Omega$ )
- The calculation speed is accelerated with MATLAB/Simulink coder and OpenGL
  - Area calculation with OpenGL : 1 DB generation takes about 4 min.
  - 1 year simulation with 10 second time interval takes about 5 min

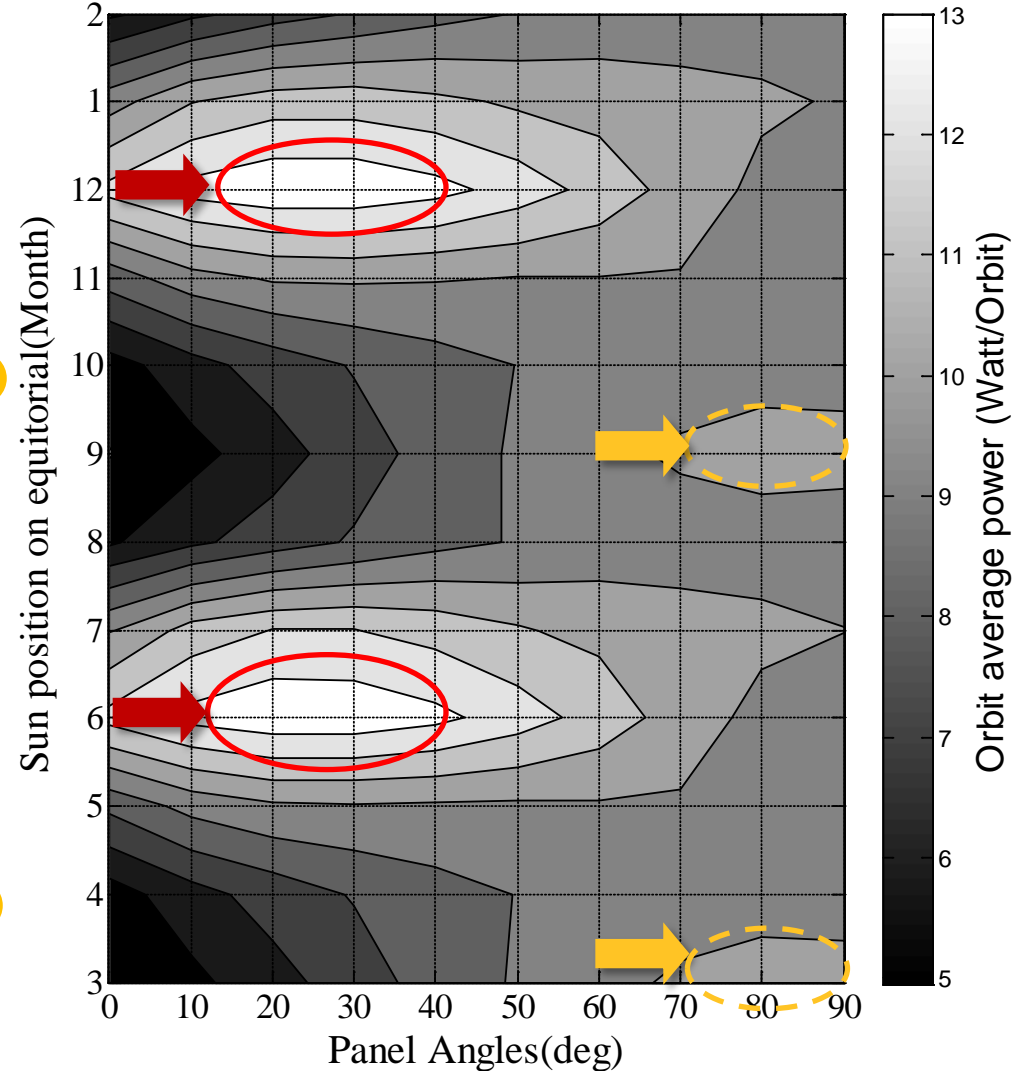
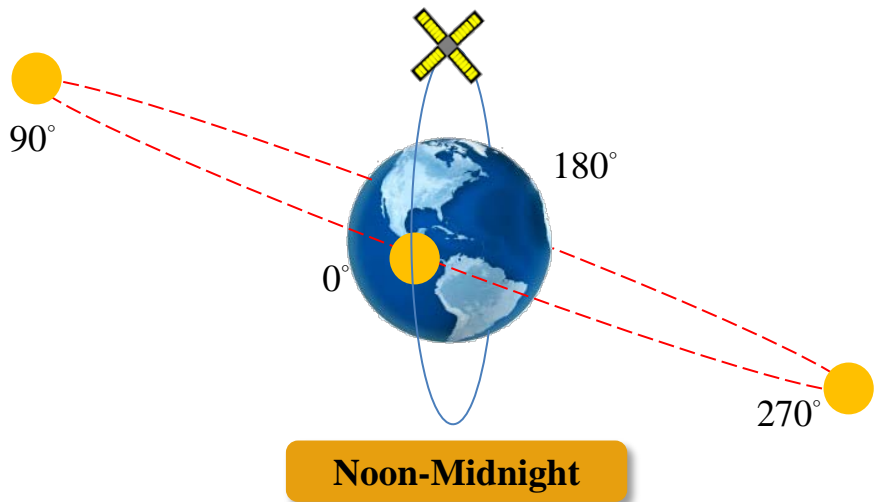
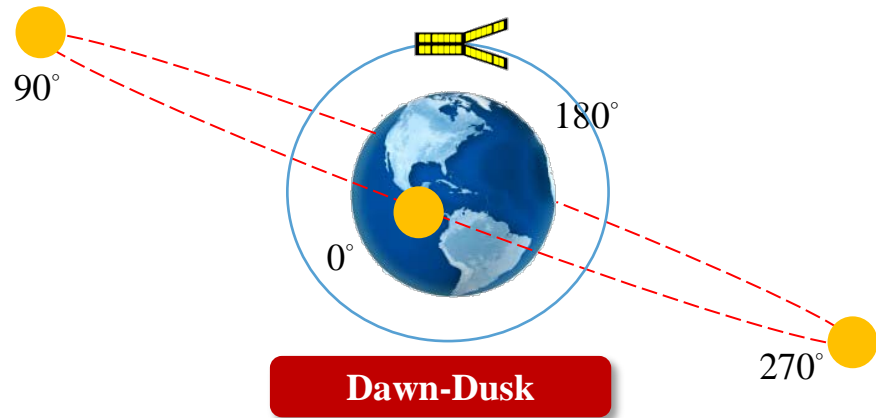
$$O_p = \begin{bmatrix} e \\ a \\ i \\ \Omega \\ \omega \\ \nu \end{bmatrix} \Rightarrow \begin{bmatrix} i \\ \Omega \end{bmatrix}$$



# Panel angle optimization of the Sun-synchronous orbit

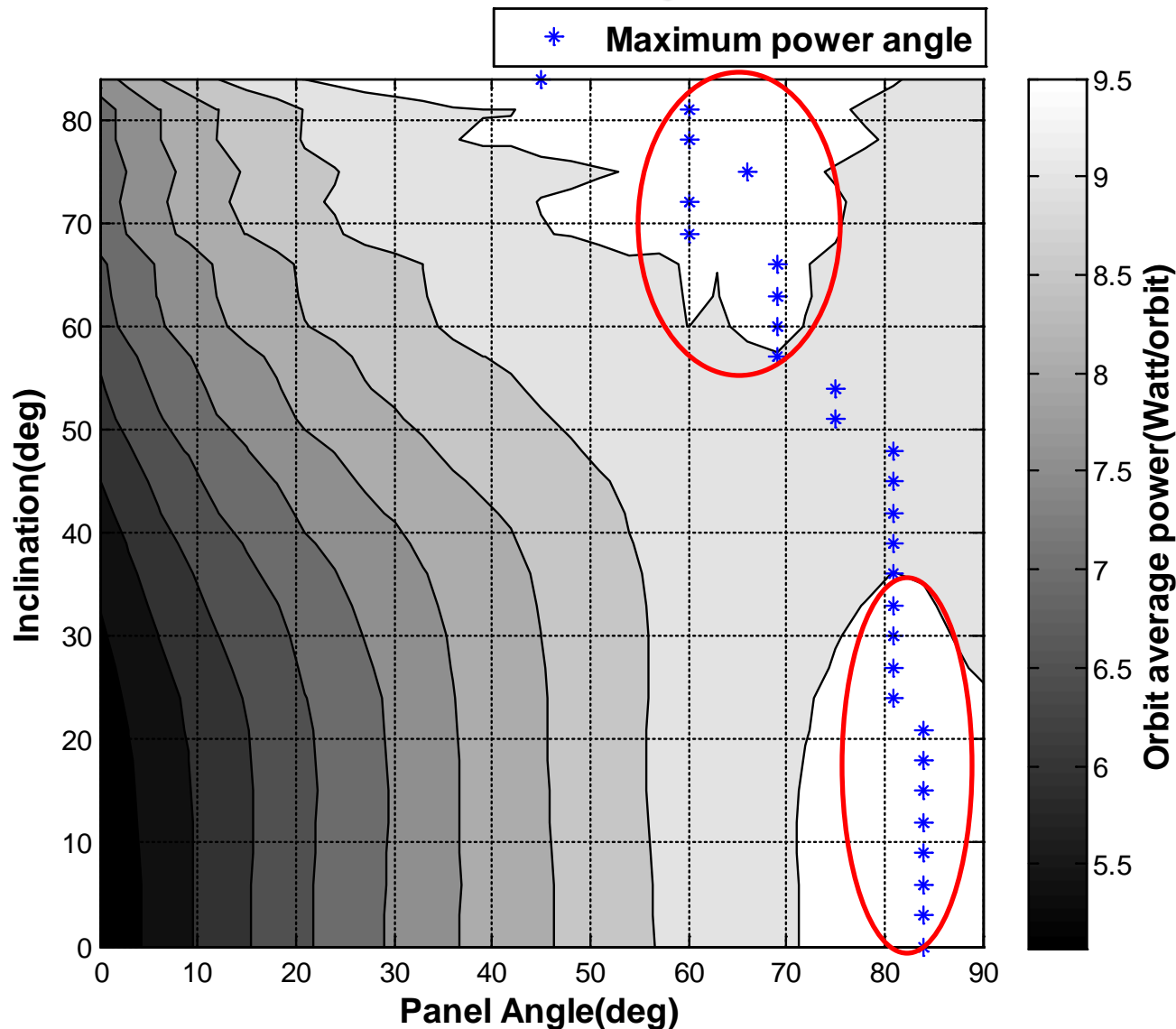
(Altitude : 700km, Inclination : 98°, Launch :3-20-2013)

Sun synchronous orbit



# Panel angle optimization of the Non Sun-synchronous orbit

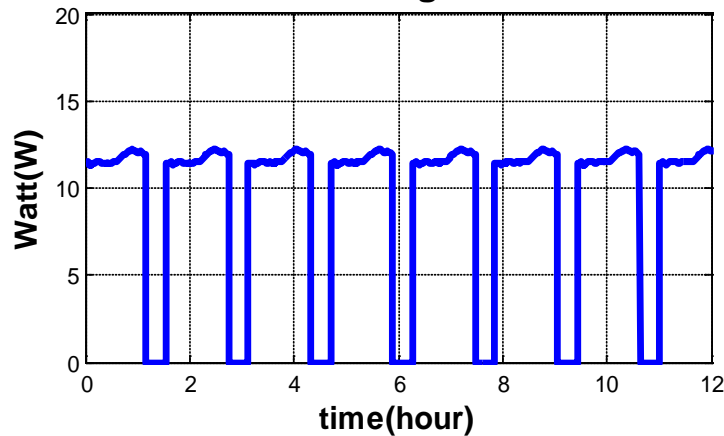
- Panel angle :  $0^\circ \sim 90^\circ$
- Inclination :  $0^\circ \sim 82^\circ$
- In the given inclination range, the moving speed of RAAN( $\Omega$ ) is greater than  $360^\circ/1\text{year}$ 
  - Then we can rule out the RAAN( $\Omega$ ) effect and compare the inclination and the panel angle's relation.



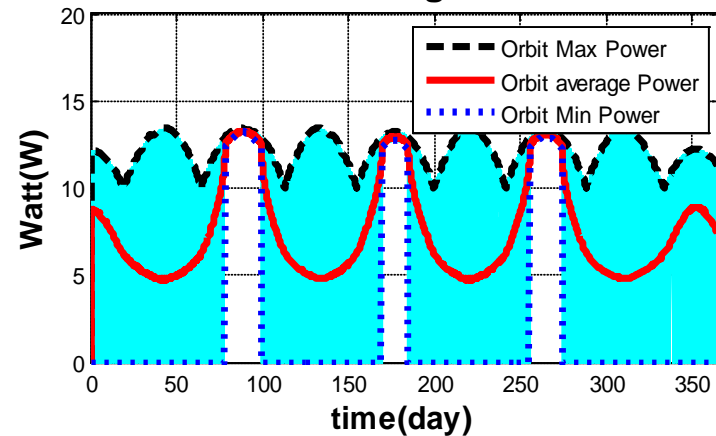
# Result Analysis of Non Sun-Synchronous orbit (Inclination : 67°)

- Small panel angle has smaller daily deviation of the power than the large panel angle
- However, Large panel angle has smaller yearly deviation of the orbit average power than small panel angle

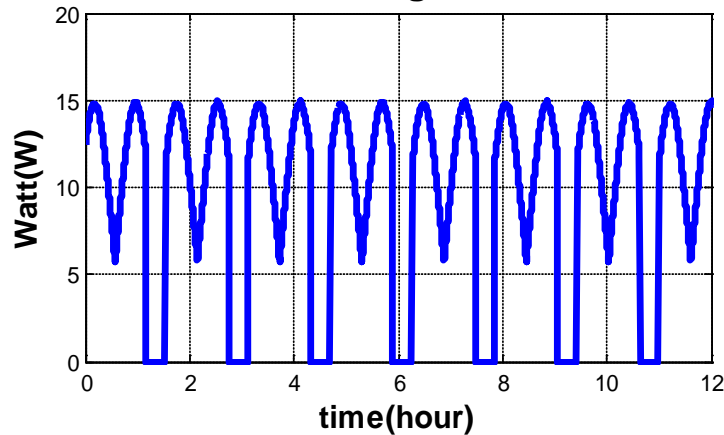
Panel angle : 0°



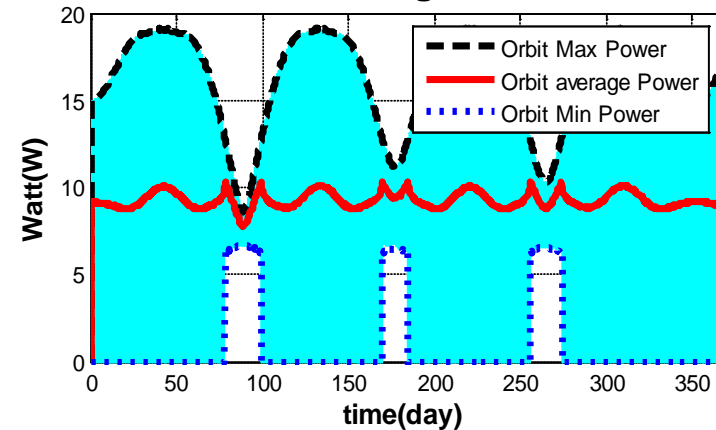
Panel angle : 0°



Panel angle : 90°



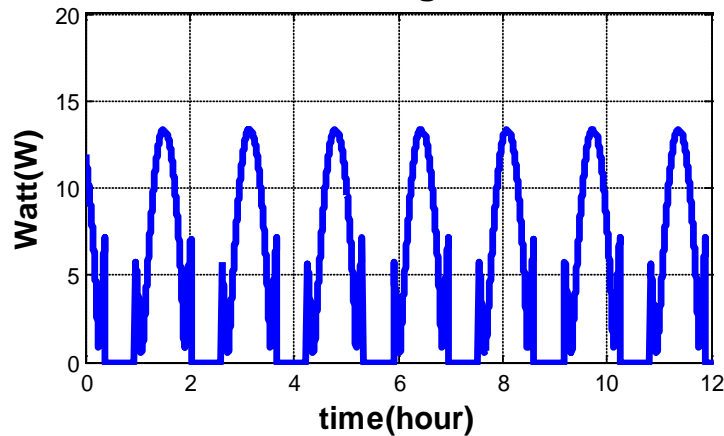
Panel angle : 90°



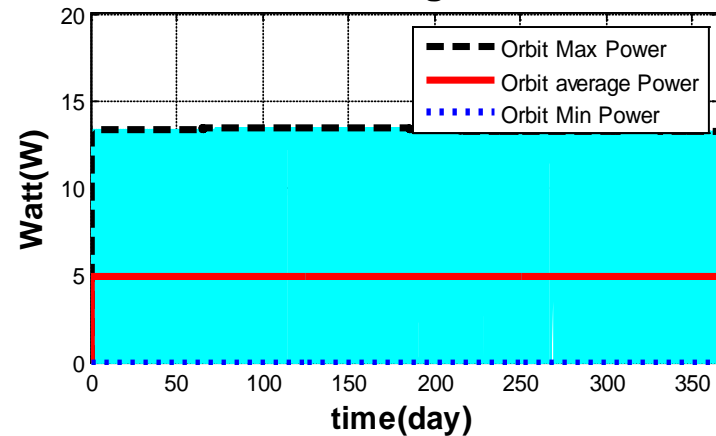
# Result Analysis of Sun-Synchronous orbit ('Noon-Midnight' Orbit)

- Altitude : 700km , Inclination : 98° , Launching date : 3-20-2015
- During 1 year, the orbit average power has no change.

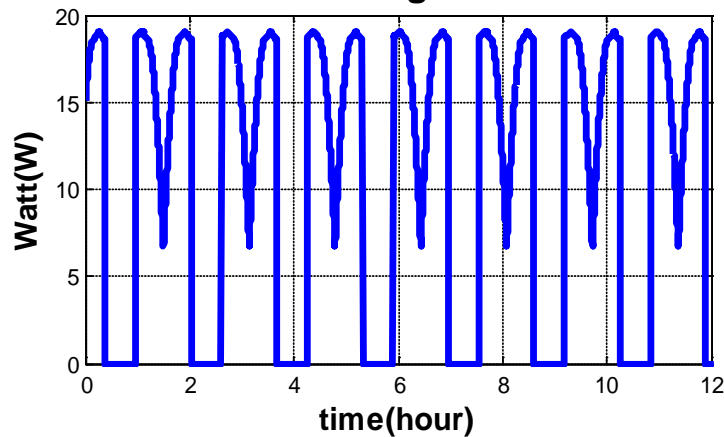
Panel angle : 0°



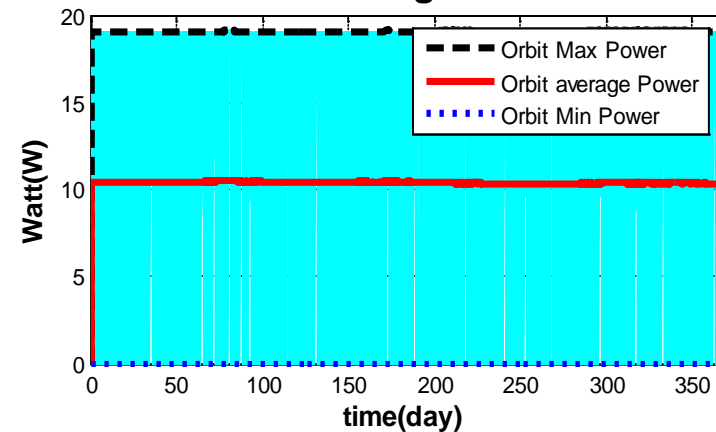
Panel angle : 0°



Panel angle : 90°



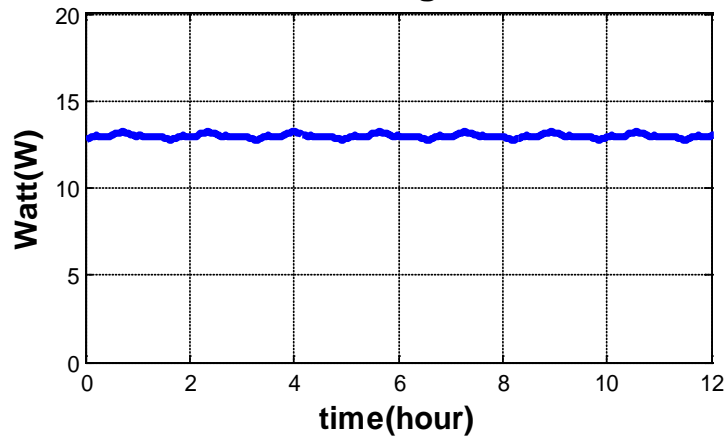
Panel angle : 90°



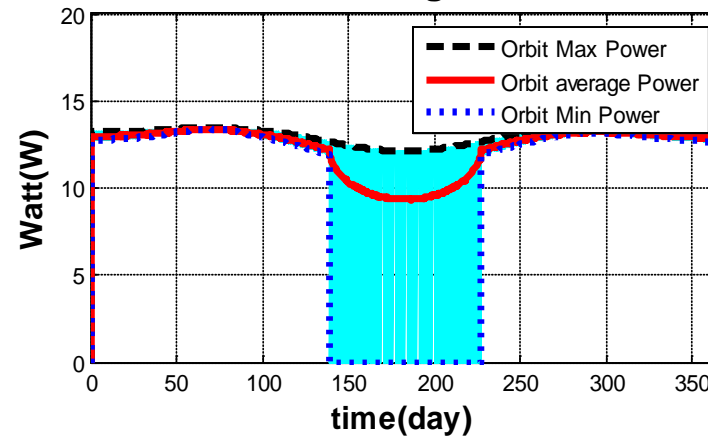
# Result Analysis of Sun-Synchronous orbit ('Dawn-Dusk' Orbit)

- Altitude : 700km, Inclination : 98°, Launching date : 6-20-2015
- If altitude is  $\geq 1,060$ km, the eclipse period will not appear.

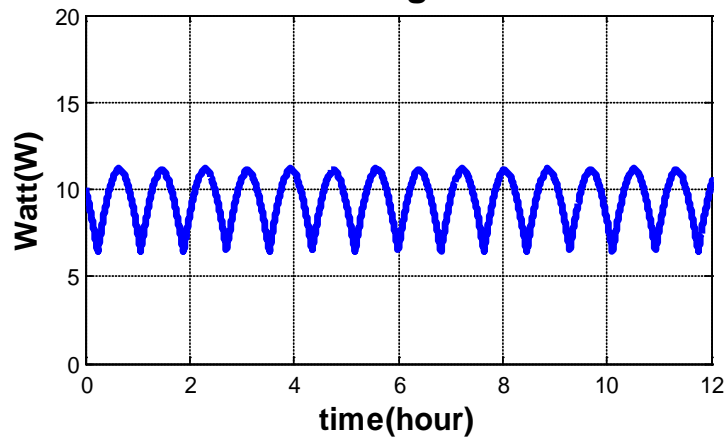
Panel angle : 0°



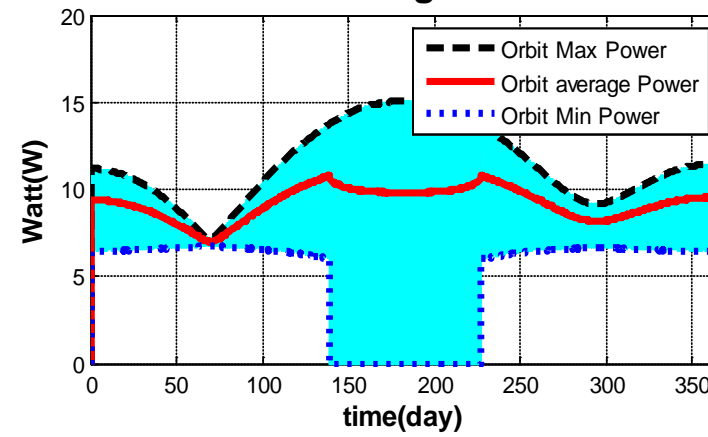
Panel angle : 0°



Panel angle : 90°



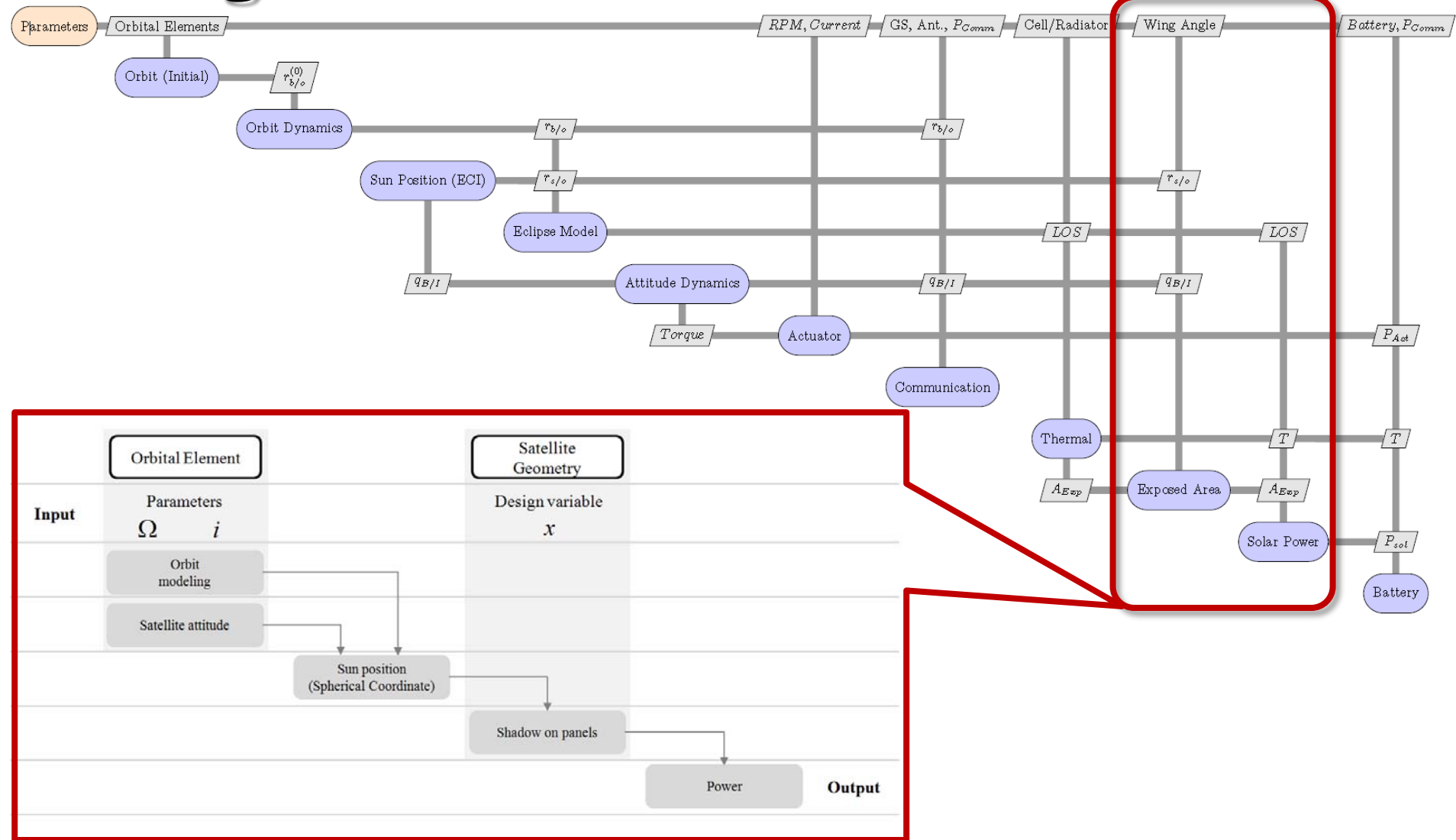
Panel angle : 90°



# Conclusions

- **Advanced panel angle design optimization technique**
  - **Based on the result of the numerical simulation of every possible condition**
  - **Shadow effects consider**
    - Deployable panels to other deployable panels
    - Deployable panels to the body panels
  - **Dynamics consider**
    - Orbit dynamics with J2, J3, J4.
    - Attitude dynamics
- **Future work : EPS design optimization**
  - **Solar cell IV curve characteristic Modeling**
  - **Cell/Radiator thermal characteristics.**
  - **Battery characteristic**
  - **Albedo consideration**
- **Large scale Multidisciplinary Design Optimization(MDO) of Cubesat**
  - **Because the running all possible case simulation is very exhaustive and not practical**
  - **Researching ‘Gradient based optimization’**

# Large Scale Cubesat MDO

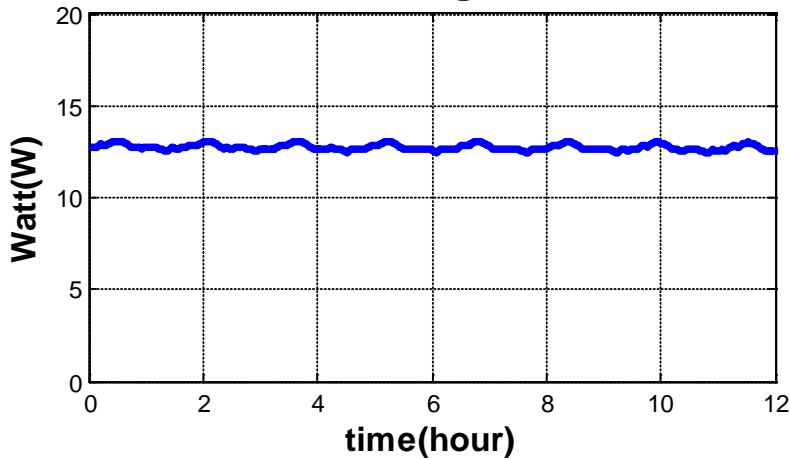




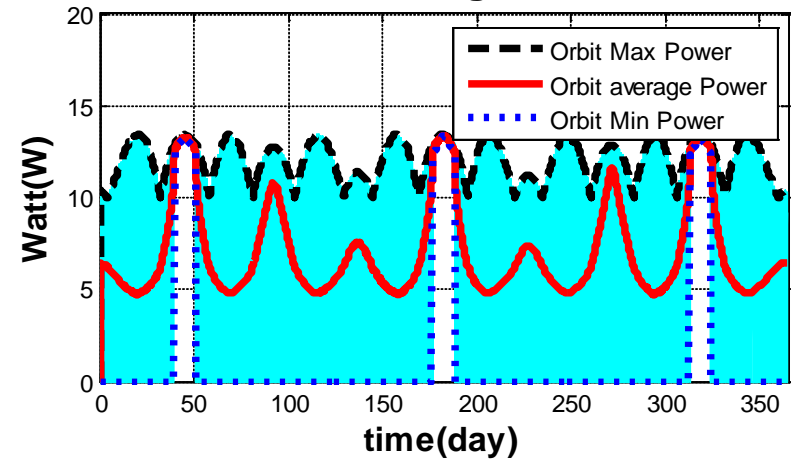
# Result Analysis of Non Sun-Synchronous orbit (Inclination : 67°)

- Day = 50

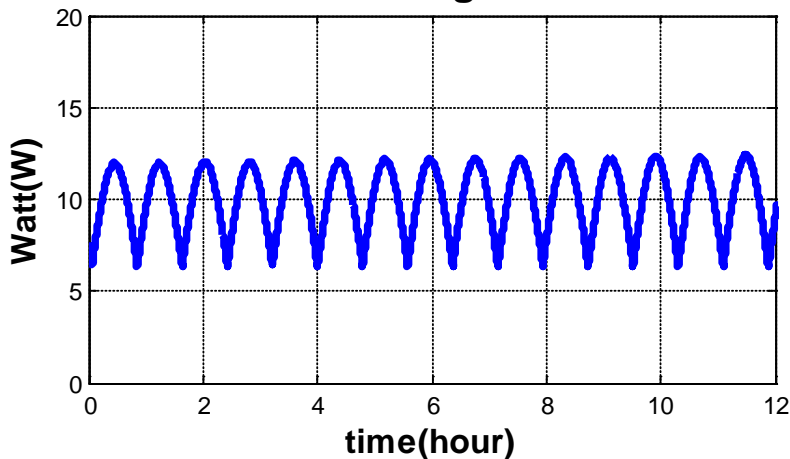
Panel angle : 0°



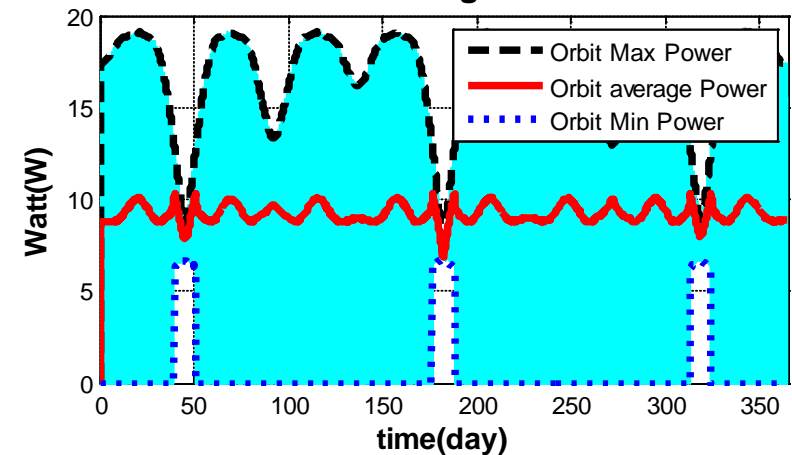
Panel angle : 0°



Panel angle : 0°

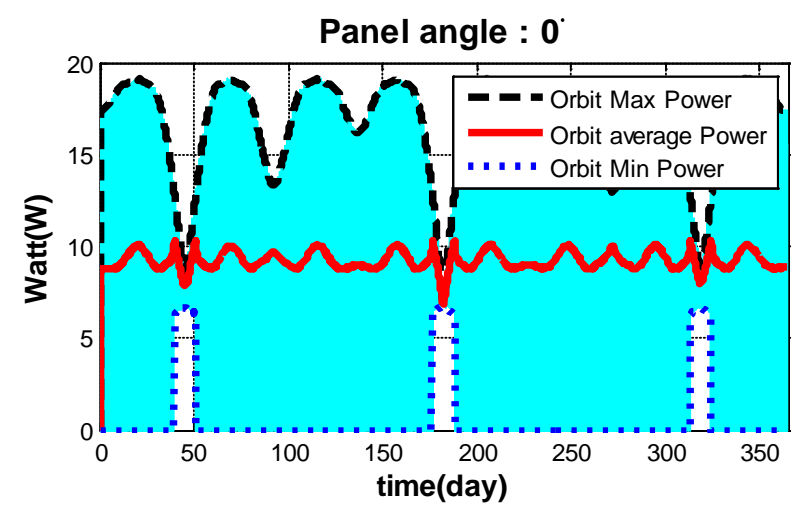
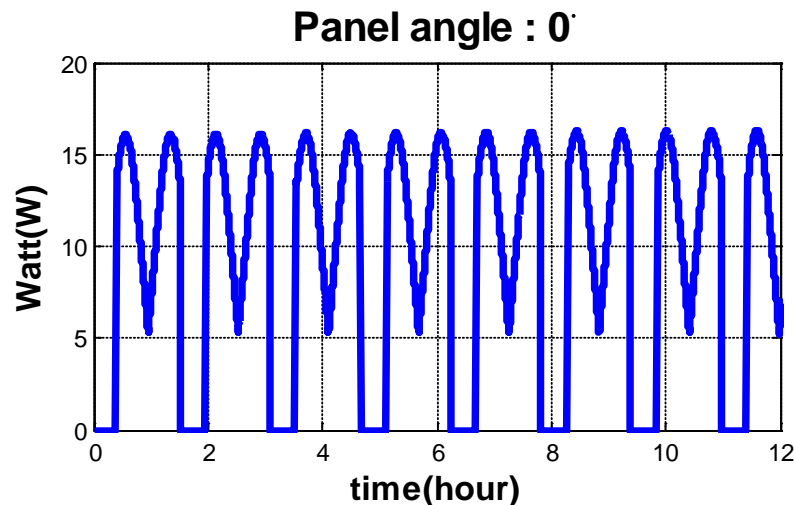
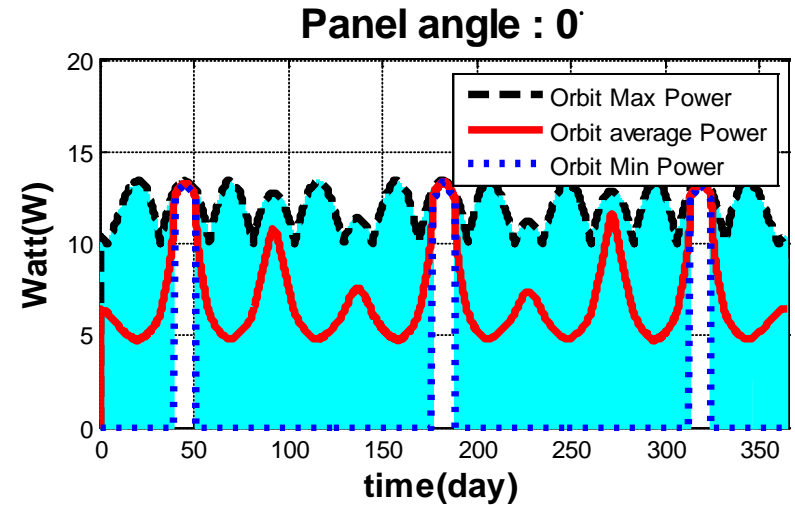
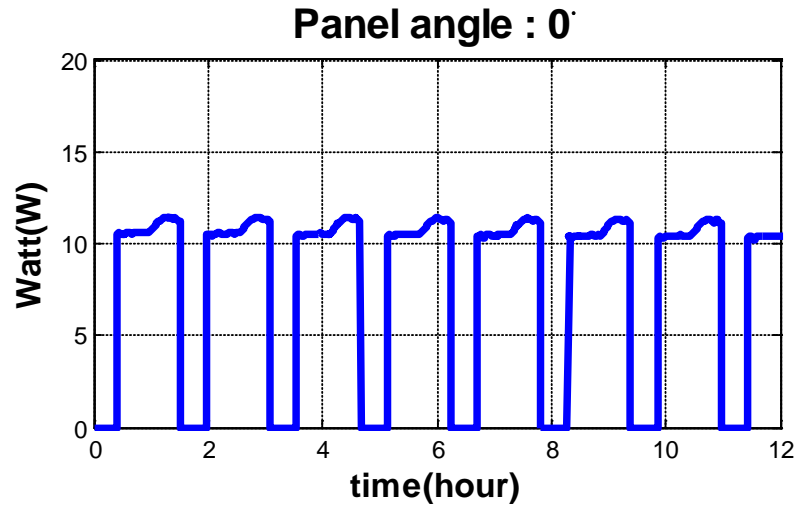


Panel angle : 0°



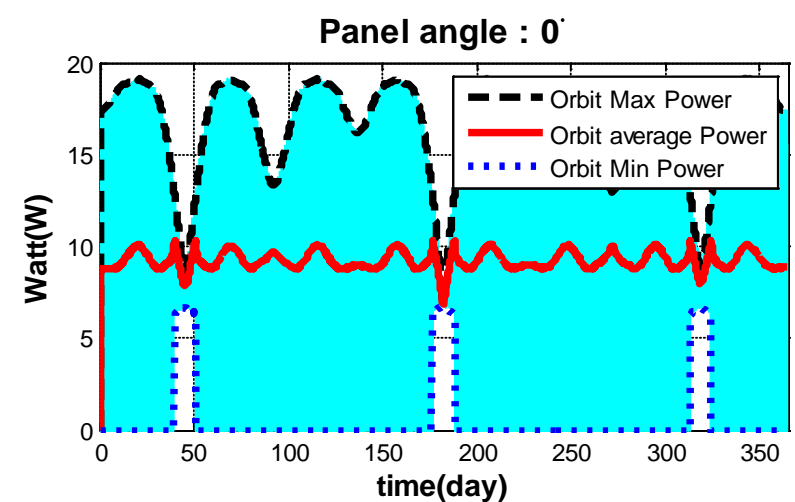
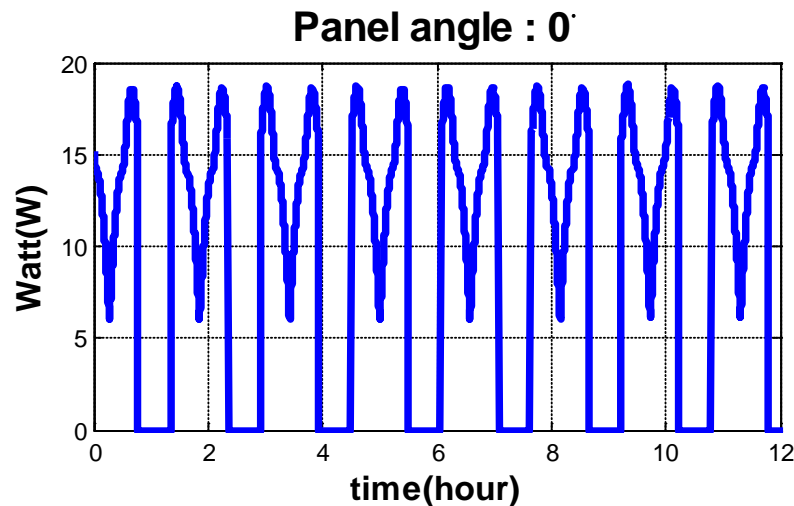
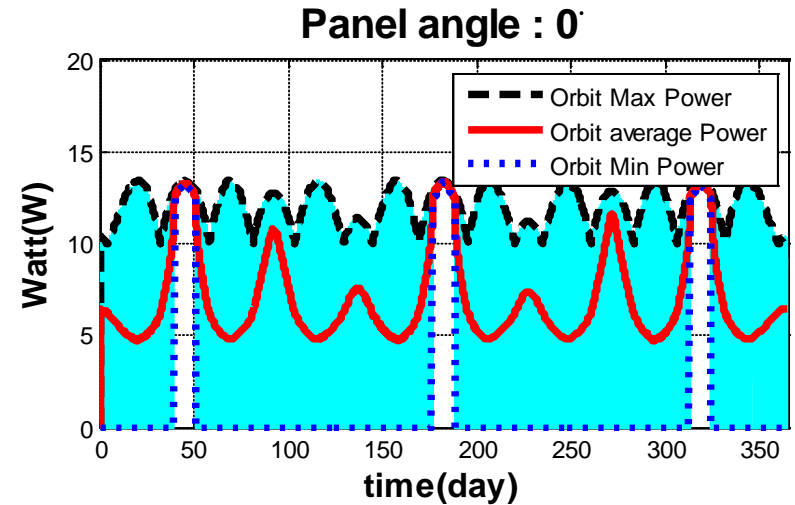
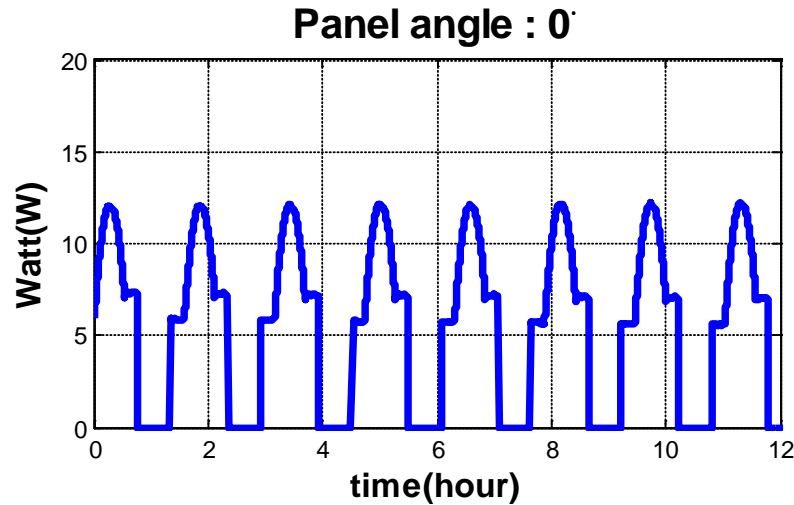
# Result Analysis of Non Sun-Synchronous orbit (Inclination : 67°)

- Day = 100



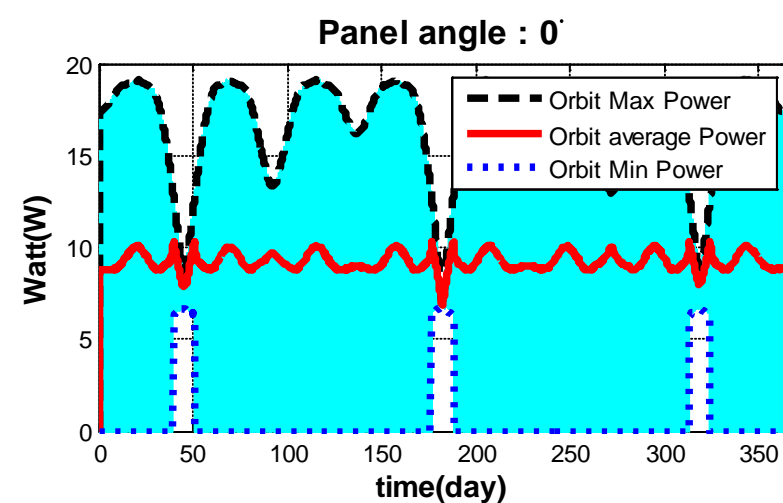
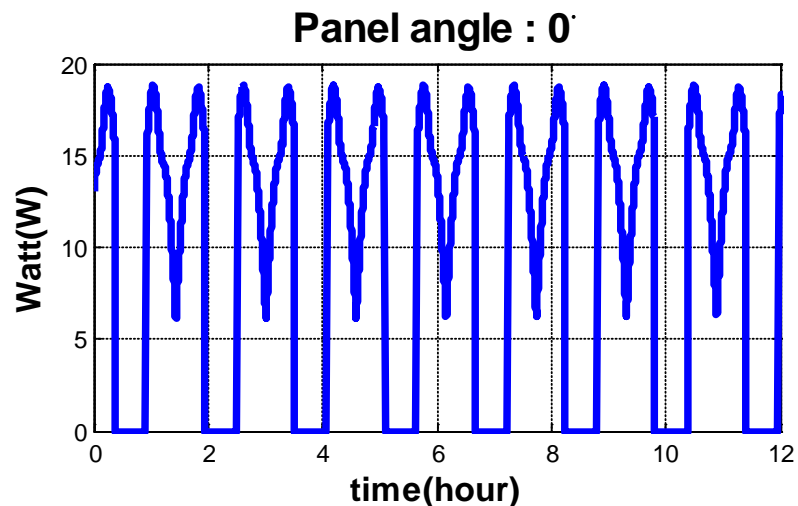
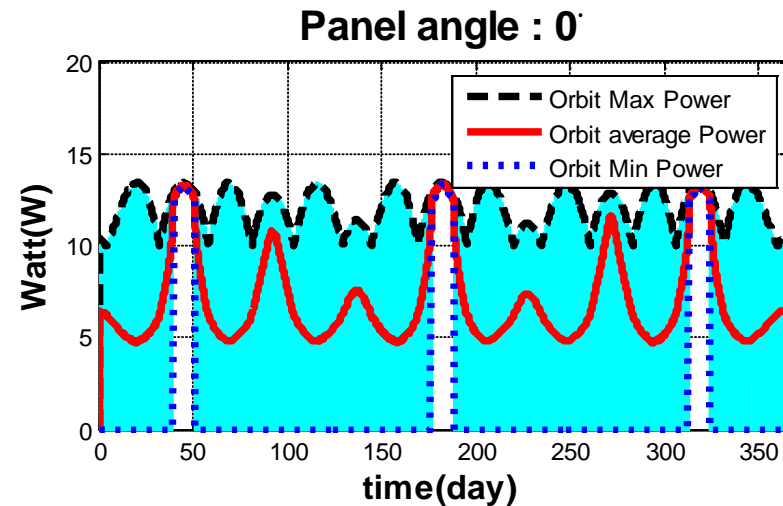
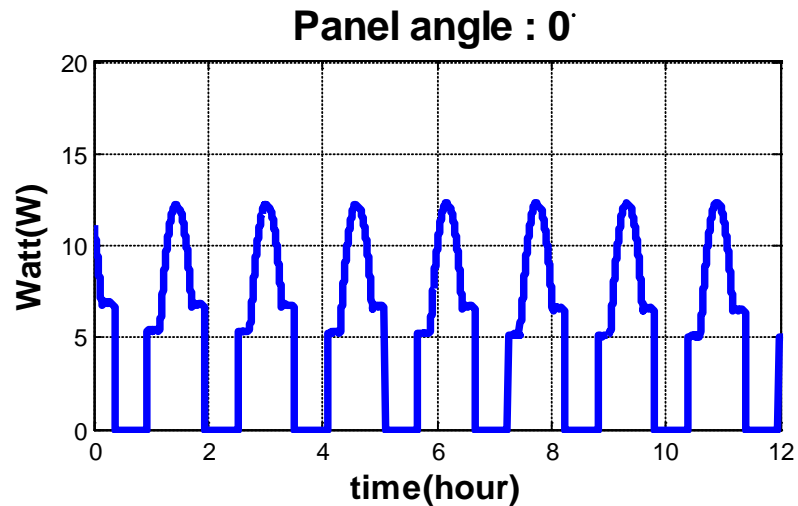
# Result Analysis of Non Sun-Synchronous orbit (Inclination : 67°)

- Day = 150



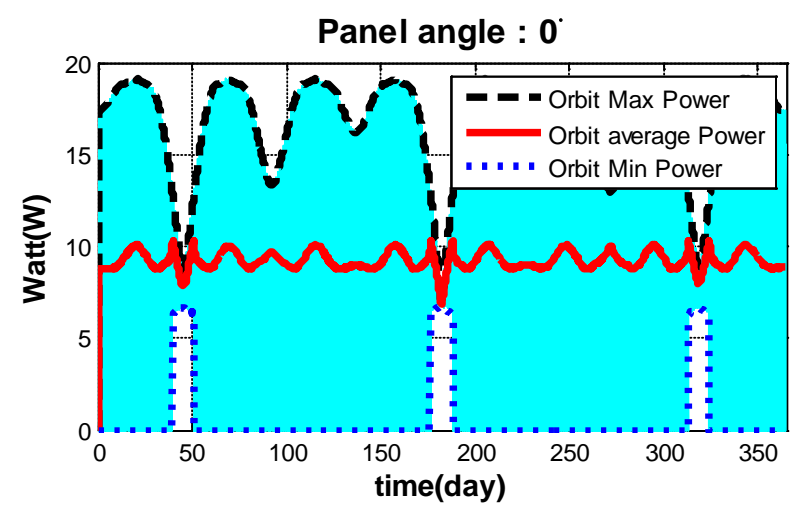
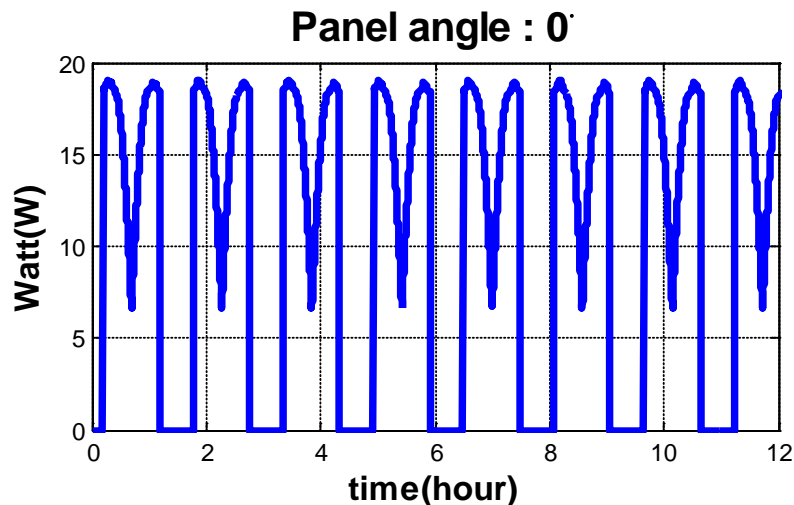
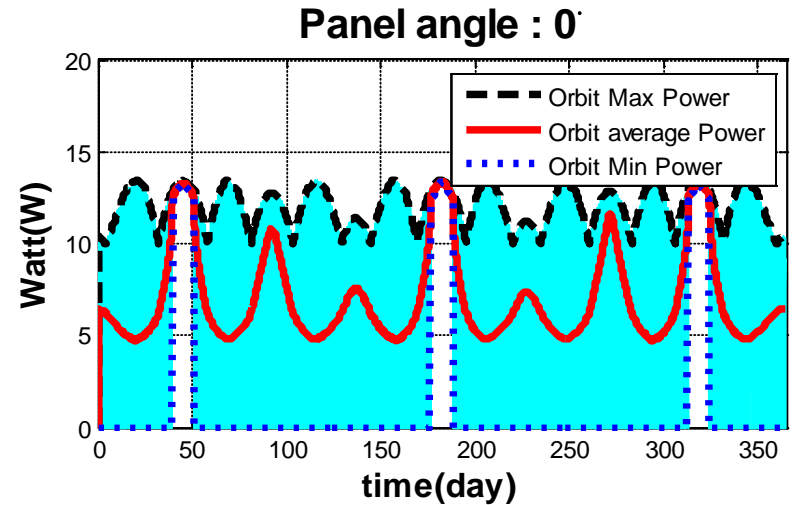
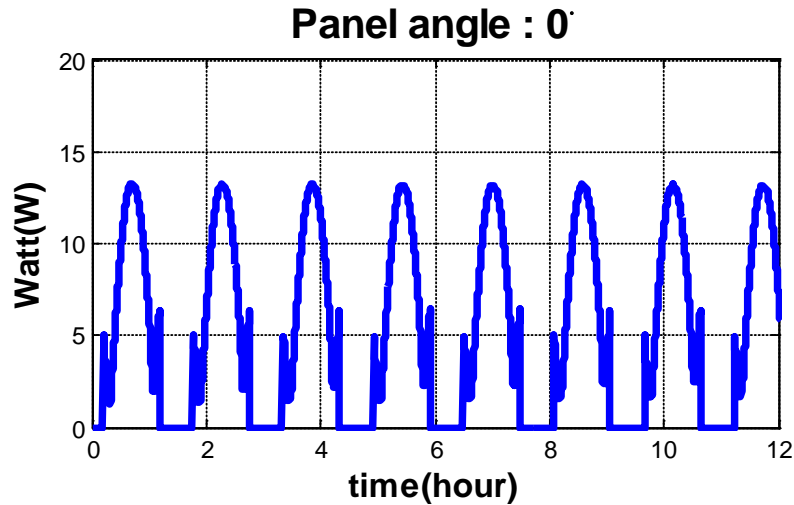
# Result Analysis of Non Sun-Synchronous orbit (Inclination : 67°)

- Day = 200



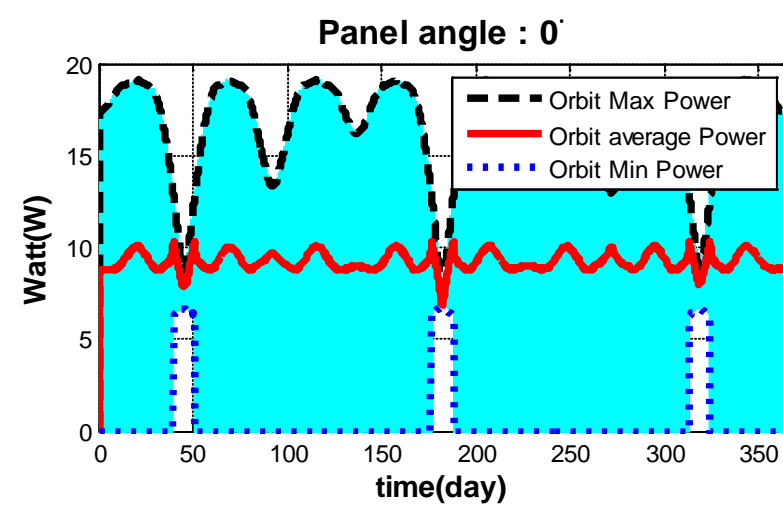
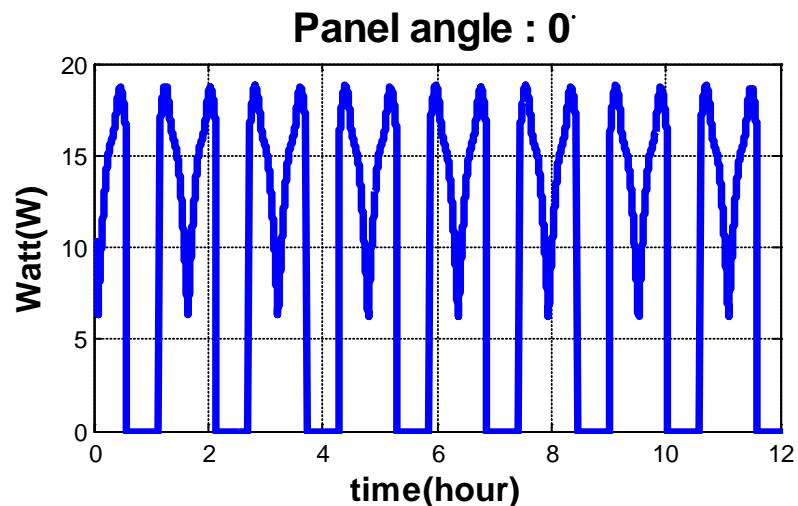
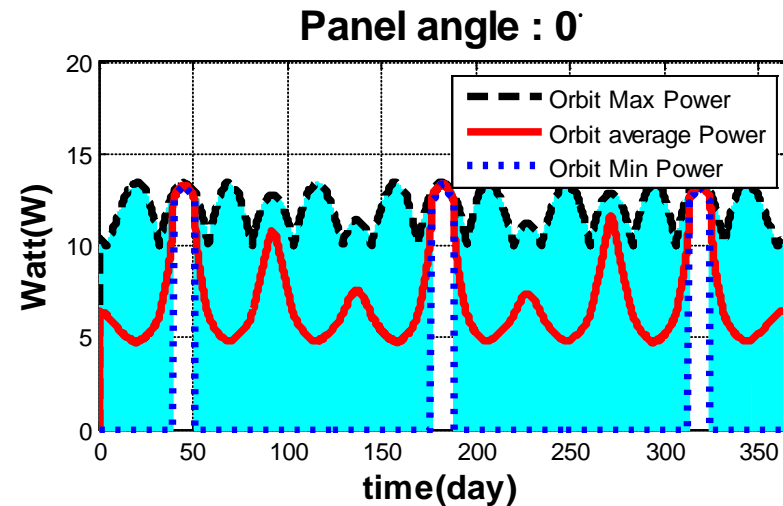
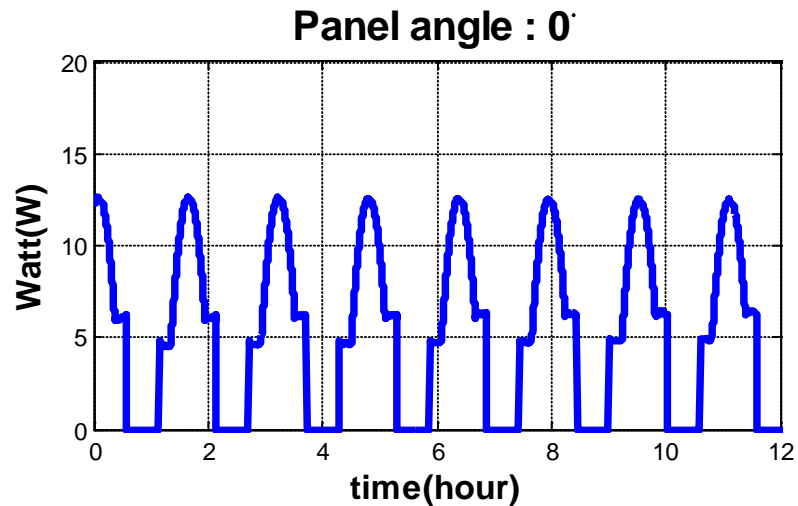
# Result Analysis of Non Sun-Synchronous orbit (Inclination : 67°)

- Day = 250



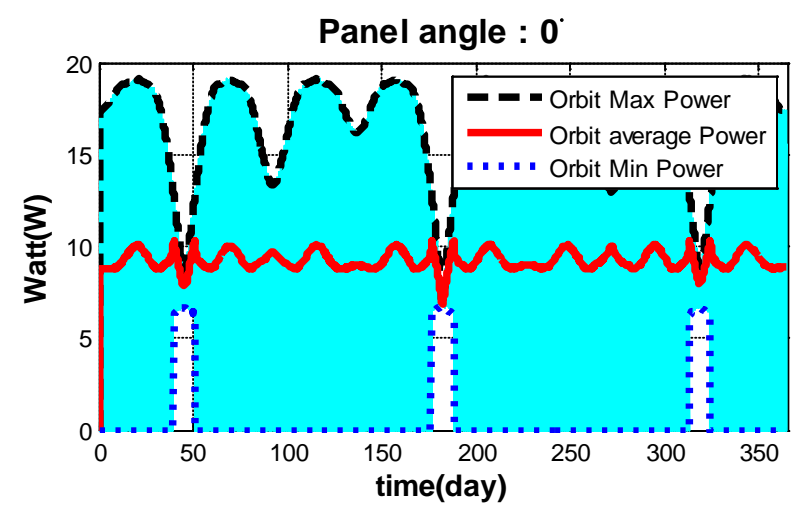
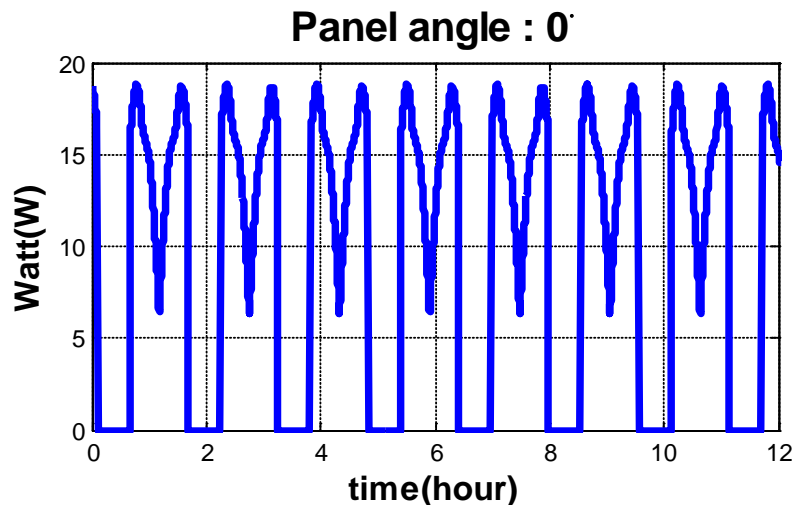
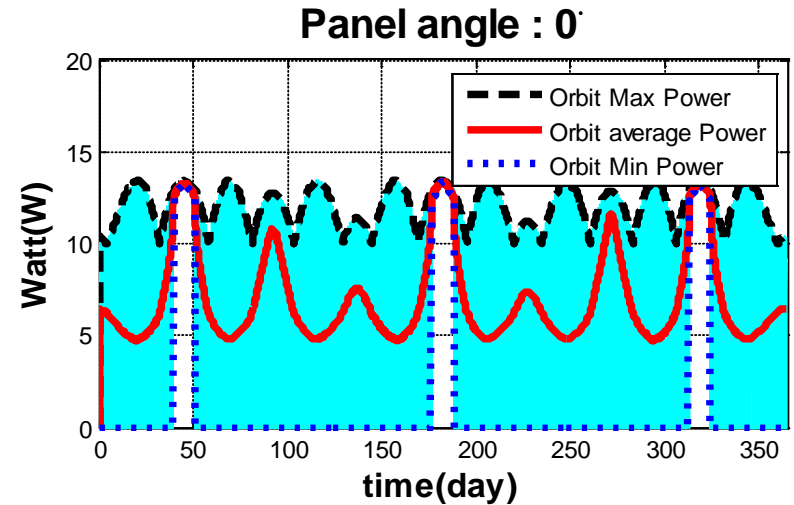
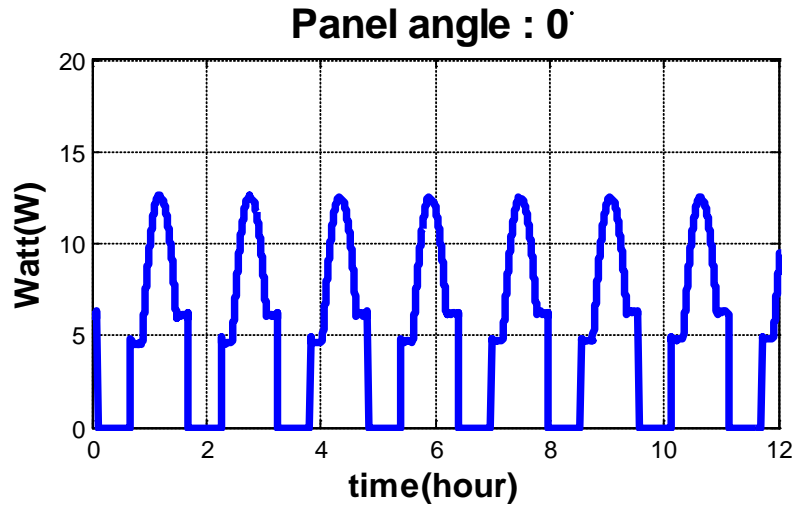
# Result Analysis of Non Sun-Synchronous orbit (Inclination : 67°)

- Day = 300



# Result Analysis of Non Sun-Synchronous orbit (Inclination : 67°)

- Day = 350

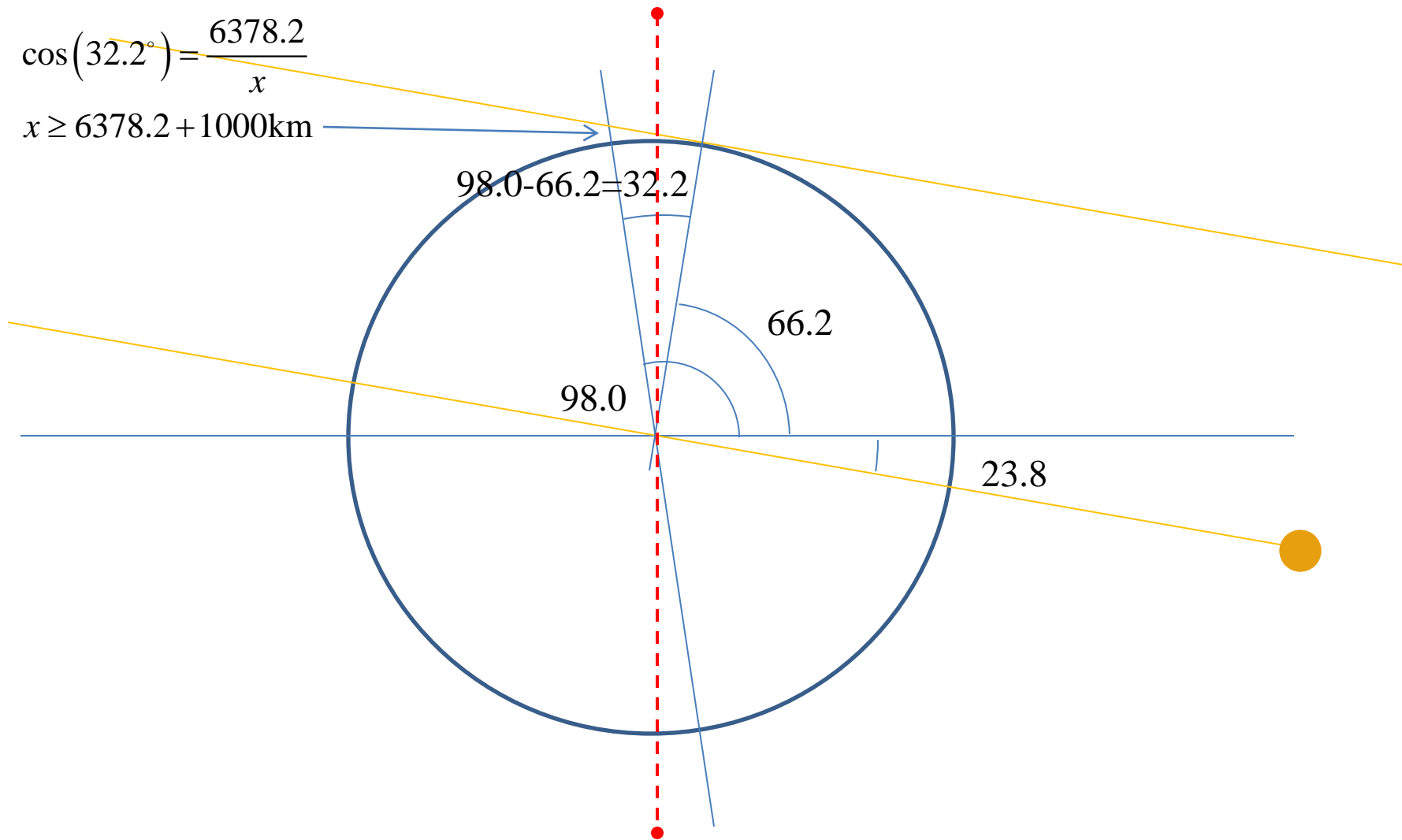




# Eclipse of the Dawn-Dusk, in the Low Earth Orbit

$$\cos(32.2^\circ) = \frac{6378.2}{x}$$

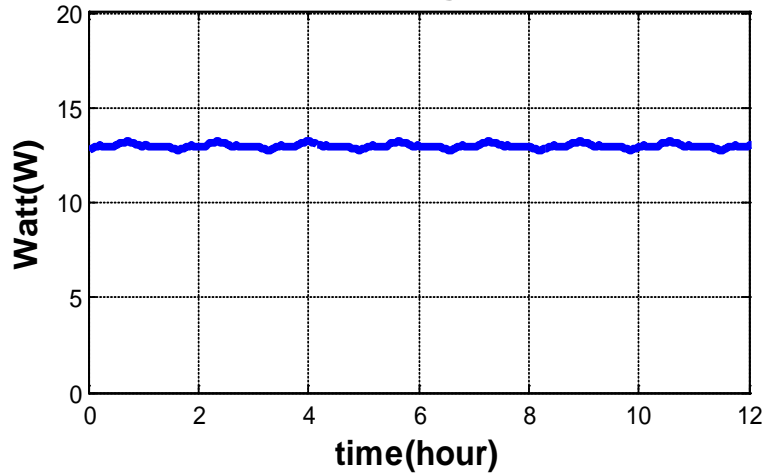
$$x \geq 6378.2 + 1000\text{km}$$



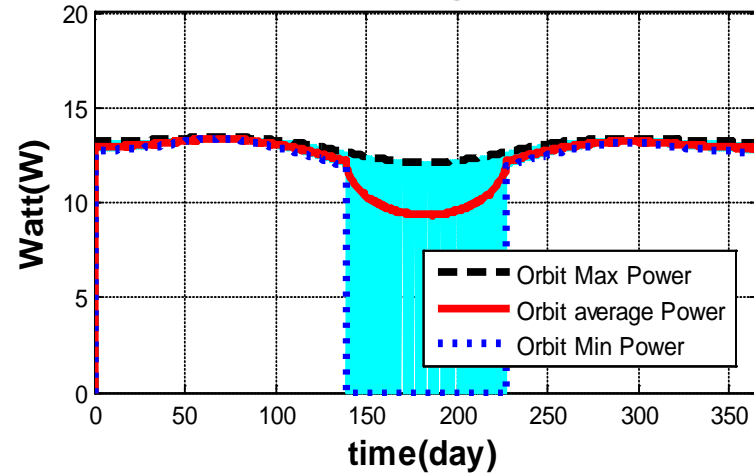
# Result Analysis of Sun-Synchronous orbit ('Dawn-Dusk')

- Comparison between different angles

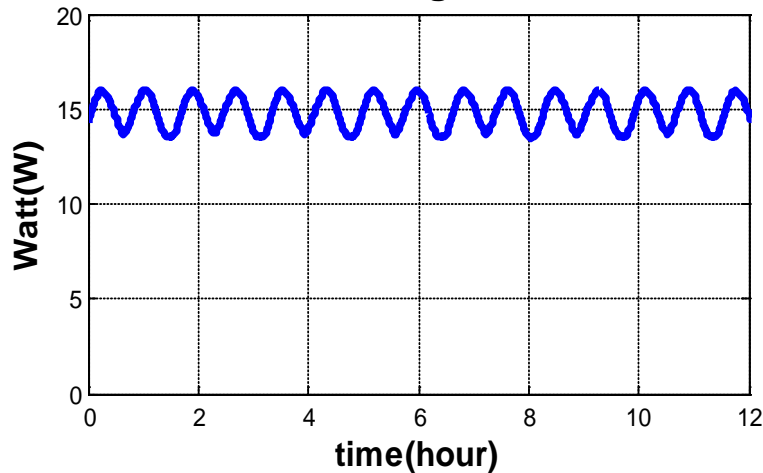
Panel angle : 0°



Panel angle : 0°



Panel angle : 23°



Panel angle : 23°

